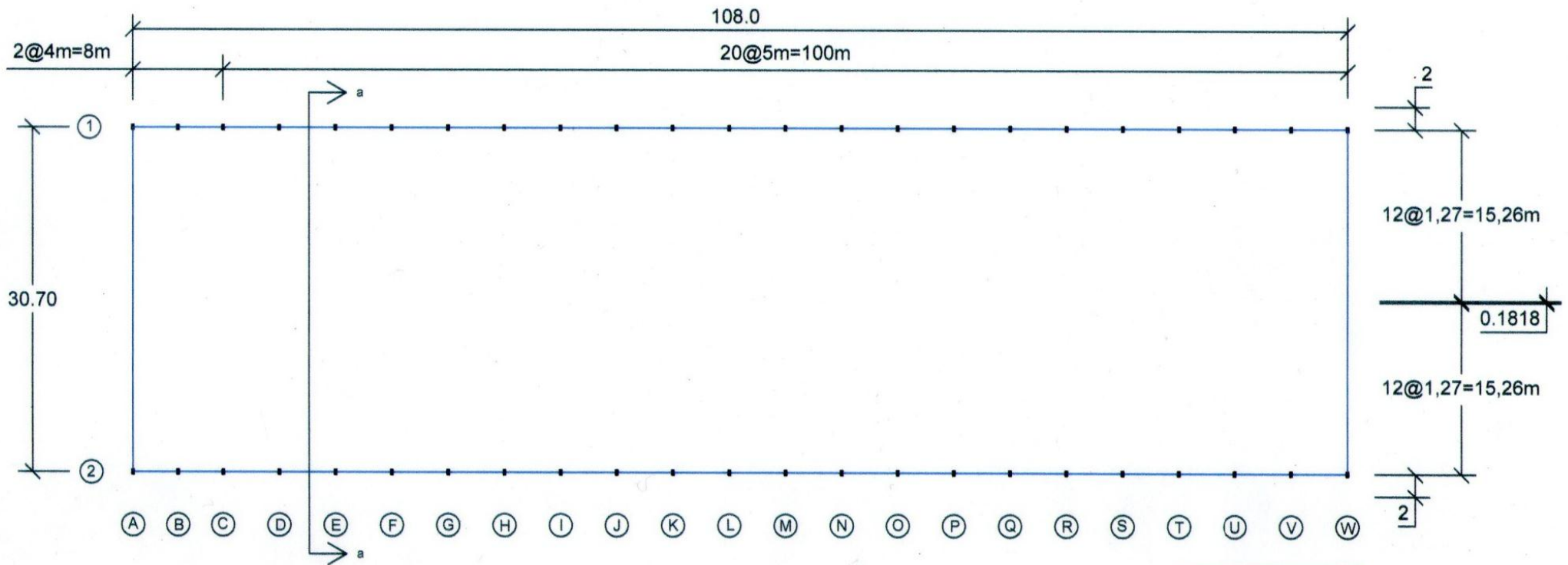


Lampiran 1. Denah



DENAH

Skala: 0 800 1600
400 1200 2000 cm

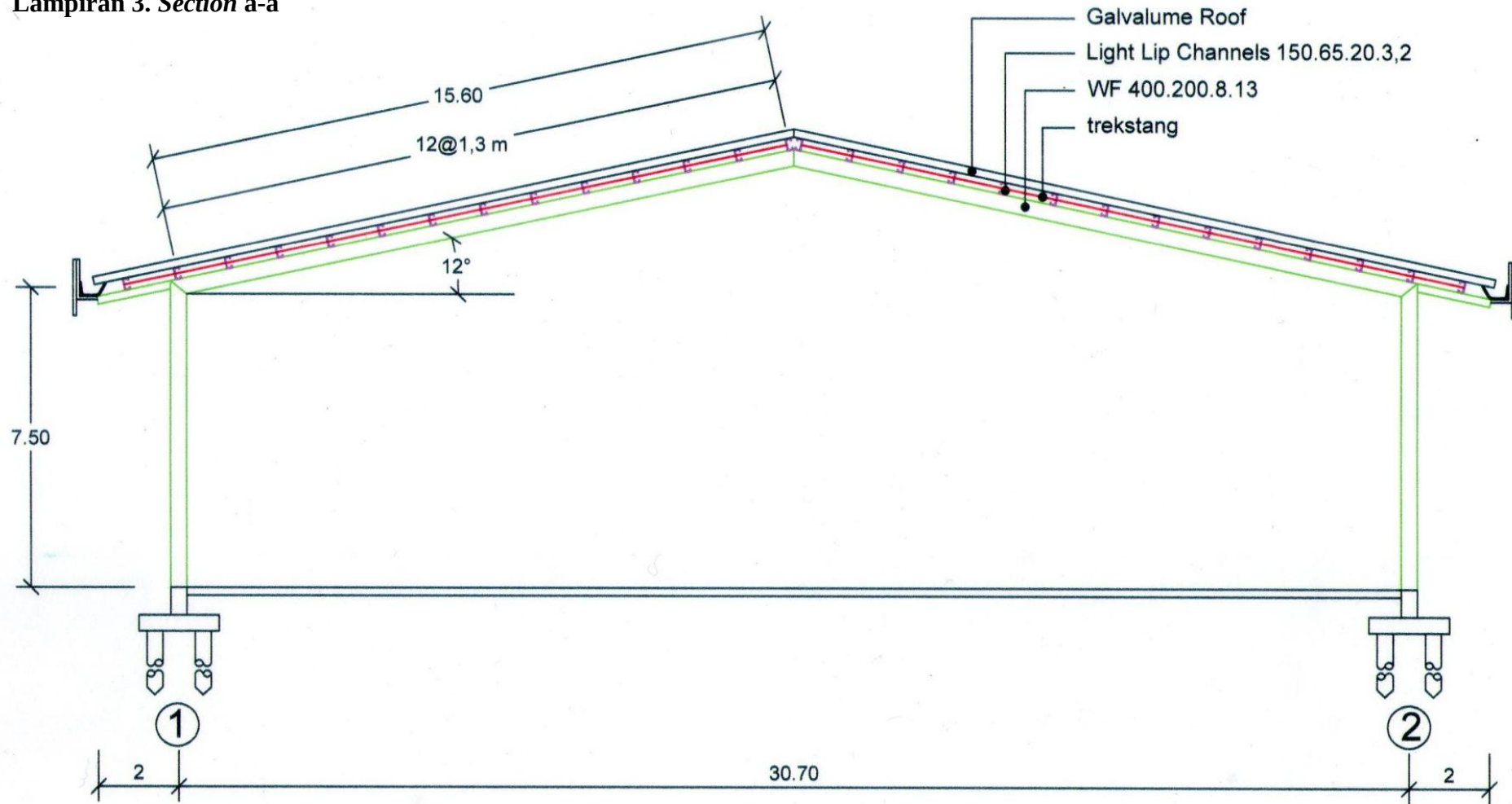
Keterangan:

— kolom
— dinding

Lampiran 2. Roof Plan



Lampiran 3. Section a-a



Section a-a

Skala: 0 200 400 100 300 500 cm



Lampiran 4. Perencanaan Gording

A. Perencanaan Gording

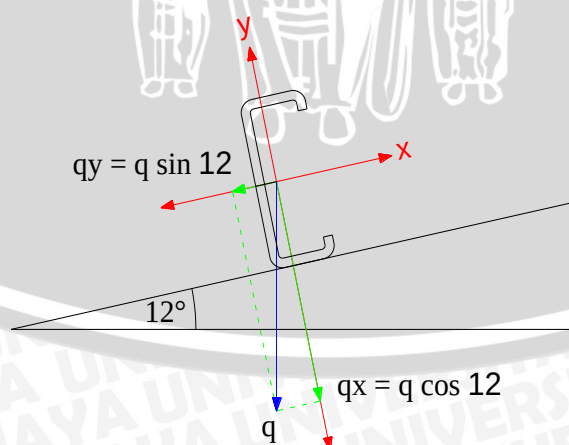
A.1 Data perencanaan & spesifikasi profil gording

Data-data yang diperlukan untuk merencanakan sebuah gording antara lain:

- Jarak antar gording = 1,3 m
- Jarak antar kuda-kuda = 5 m
- Sudut kemiringan atap = 12°
- Berat penutup atap = 11 kg/m²
- Tekanan angin = 25 kg/m²

Profil yang dipakai: Light Lip Channels 150.65.20.3,2

- A = 150 mm
- B = 65 mm
- t = 3.2 mm
- Luas penampang = 9,567 cm²
- Berat = 7,51 kg/m
- $I_x = 332 \text{ cm}^4$
- $I_y = 53,8 \text{ cm}^4$
- $Z_x = 44,3 \text{ cm}^3$
- $Z_y = 12,2 \text{ cm}^3$
- $i_x = 5,89 \text{ cm}$
- $i_y = 2,37 \text{ cm}$



Penguraian Beban



A.2 Pembebanan Gording

A.2.1 Beban Pada Gording

a) Beban Mati (D)

$$\begin{aligned}
 & - \text{Berat sendiri gording} & = & 7,51 \\
 & - \text{Berat penutup atap} & = & 11 \times 1,3 = 14,30 + \\
 & & & 21,81 \\
 & - \text{Berat alat sambung} & = & 10\% \times 21,81 = 2,18 + \\
 & \text{Total beban mati} & = & 24,0 \text{ kg/m}
 \end{aligned}$$

Penguraian beban

$$\begin{aligned}
 q_x &= \text{Total beban mati} \times \cos 12^\circ \\
 &= 24,0 \times 0,978 \\
 &= 23 \text{ kg/m}
 \end{aligned}$$

$$\begin{aligned}
 V_x &= 0,5 \cdot q_x \cdot L \\
 &= 0,5 \times 23 \times 5 \\
 &= 59 \text{ kg}
 \end{aligned}$$

$$\begin{aligned}
 M_x &= q_x \cdot L^2 / 8 \\
 &= 23 \times 25 / 8 \\
 &= 73 \text{ kgm}
 \end{aligned}$$

$$\begin{aligned}
 q_y &= \text{Total beban mati} \times \sin 12^\circ \\
 &= 24,0 \times 0,208 \\
 &= 5 \text{ kg/m}
 \end{aligned}$$

$$\begin{aligned}
 V_y &= 0,5 \cdot q_y \cdot L \\
 &= 0,5 \times 5 \times 1,67 \\
 &= 4 \text{ kg}
 \end{aligned}$$

$$\begin{aligned}
 M_y &= q_y \cdot L^2 / 8 \\
 &= 5 \times 2,78 / 8 \\
 &= 2 \text{ kgm}
 \end{aligned}$$

b) Beban Hidup akibat Pekerja (La)

Beban hidup pada atap dan atau pada bagian atap serta pada struktur tudung (canopi) yang dapat dipakai dan dibebani oleh orang harus diambil minimum sebesar 100 kg bidang datar

Penguraian beban

$$\begin{aligned}
 P_x &= \text{beban pekerja} \times \cos 12^\circ \\
 &= 100 \times 0,978 \\
 &= 98 \text{ kg}
 \end{aligned}$$

$$\begin{aligned}
 V_x &= 0,5 \cdot P_x \\
 &= 0,5 \times 98 \\
 &= 49 \text{ kg}
 \end{aligned}$$

$$\begin{aligned} M_x &= P_x \cdot L / 4 \\ &= 98 \times 5 / 4 \\ &= 122 \text{ kgm} \end{aligned}$$

$$\begin{aligned} P_y &= \text{beban pekerja} \times \sin 12^\circ \\ &= 100 \times 0,208 \\ &= 21 \text{ kg} \end{aligned}$$

$$\begin{aligned} V_y &= 0,5 \cdot P_y \\ &= 1 \times 21 \\ &= 10 \text{ kg} \end{aligned}$$

$$\begin{aligned} M_y &= P_y \cdot L / 4 \\ &= 21 \times 1,67 / 4 \\ &= 9 \text{ kgm} \end{aligned}$$

c) Beban Angin (W)

$$\begin{aligned} c_1 &= \text{koef. Angin tekan} \\ &= 0,02 \times \alpha - 0,4 \\ &= 0,02 \times 12 - 0,4 \\ &= -0,16 \end{aligned}$$

$$\begin{aligned} c_2 &= \text{koef. Angin hisap} \\ &= -0,4 \end{aligned}$$

Beban angin pada atap

$$\begin{aligned} q \text{ tekan} &= c_1 \times 25 \times \text{jarak antar kuda-kuda} \times \cos \alpha \\ &= -20 \text{ kg/m} \end{aligned}$$

$$\begin{aligned} q \text{ hisap} &= c_2 \times 25 \times \text{jarak antar kuda-kuda} \times \cos \alpha \\ &= -49 \text{ kg/m} \end{aligned}$$

$$\begin{aligned} V_x &= 0,5 \cdot q_x \cdot L \\ &= -49 \text{ kg} \end{aligned}$$

$$\begin{aligned} M_x &= q_x \cdot L^2 / 8 \\ &= -61 \text{ kgm} \end{aligned}$$

d) Beban air hujan (H)

Beban terbagi rata per m^2 bidang datar berasal dari beban air hujan sebesar $(40-0,8\alpha) \text{ kg/m}^2$ (PPIUG 1983 pasal 3.2.2.a)

$$\begin{aligned} W_a &= 40 - 0,8 \times \alpha \\ &= 40 - 0,8 \times 12 \\ &= 30 \text{ kg/m}^2 \end{aligned}$$

(tidak perlu diambil lebih besar dari 20 kg/m^2)

$$\begin{aligned} W_a \text{ pakai} &= 20 \text{ kg/m}^2 \\ q_H &= W_a \times \text{jarak gording} \\ &= 20 \times 1,3 \\ &= 26 \text{ kg/m} \end{aligned}$$

Penguraian beban

$$\begin{aligned}
 q_x &= \text{Beban air hujan} \times \cos 12^\circ \\
 &= 26 \times 0,978 \\
 &= 25 \text{ kg/m}
 \end{aligned}$$

$$\begin{aligned}
 V_x &= 0,5 \cdot q_x \cdot L \\
 &= 0,5 \times 25 \times 5 \\
 &= 64 \text{ kg}
 \end{aligned}$$

$$\begin{aligned}
 M_x &= q_x \cdot L^2 / 8 \\
 &= 25 \times 25 / 8 \\
 &= 79 \text{ kgm}
 \end{aligned}$$

$$\begin{aligned}
 q_y &= \text{Beban air hujan} \times \sin 12^\circ \\
 &= 26 \times 0,208 \\
 &= 5 \text{ kg/m}
 \end{aligned}$$

$$\begin{aligned}
 V_y &= 0,5 \cdot q_y \cdot L \\
 &= 0,5 \times 5 \times 1,67 \\
 &= 5 \text{ kg}
 \end{aligned}$$

$$\begin{aligned}
 M_y &= q_y \cdot L^2 / 8 \\
 &= 5 \times 2,78 / 8 \\
 &= 2 \text{ kgm}
 \end{aligned}$$

A.2.2 Kombinasi Pembebanan Groding

Kombinasi pembebanan untuk struktur baja bangunan gedung berdasarkan SNI 03-1729-2002, antara lain:

1. $1,4D$
2. $1,2D + 1,6L + 0,5(L_a \text{ atau } H)$
3. $1,2D + 1,6(L_a \text{ atau } H) + (\gamma_L L \text{ atau } 0,8W)$
4. $1,2D + 1,3W + \gamma_L L + 0,5(L_a \text{ atau } H)$
5. $1,2D \pm 1,0E + \gamma_L L$
6. $0,9D \pm (1,3W \text{ atau } 1,0E)$

Keterangan:

D adalah beban mati yang diakibatkan oleh berat konstruksi permanen, termasuk dinding, lantai, atap, plafon, partisi tetap, tangga, dan peralatan layan tetap

L adalah beban hidup yang ditimbulkan oleh penggunaan gedung, termasuk kejut, tetapi tidak termasuk beban lingkungan seperti angin, hujan, dan lain-lain

L_a adalah beban hidup di atap yang ditimbulkan selama perawatan oleh pekerja, peralatan, dan material, atau selama penggunaan biasa oleh orang dan benda bergerak

H adalah beban hujan, tidak termasuk yang diakibatkan genangan air

W adalah beban angin

E adalah beban gempa, yang ditentukan menurut SNI 03-1726-1989, atau penggantinya

Beban-beban dalam perencanaan gording pada bangunan ini adalah beban mati (D), beban hidup akibat pekerja (L_a), beban air hujan (H) dan beban angin (W). Nilai beban hidup akibat pekerja terhadap sumbu- x dan sumbu- y lebih besar dari nilai beban air hujan (H) sehingga yang dipakai untuk perhitungan kombinasi beban ini adalah beban hidup akibat pekerja (L_a). Berdasarkan perhitungan beban angin pada butir A.2.1(c), nilai beban angin yang didapatkan pada perhitungan angin tekan dan angin hisap memiliki nilai negatif, maka beban angin ini dapat diabaikan karena dapat memperingan struktur.

Kombinasi terhadap Sumbu- x

Kombinasi	M.D		M.La		M_x (kgm)
1	1,4	73		=	103
2	1,2	73	+	0,5 122	= 149
3	1,2	73	+	1,6 122	= 284
4	1,2	73	+	0,5 122	= 149
5	1,2	73		=	88
6	0,9	73		=	66
M_x MAX					= 284

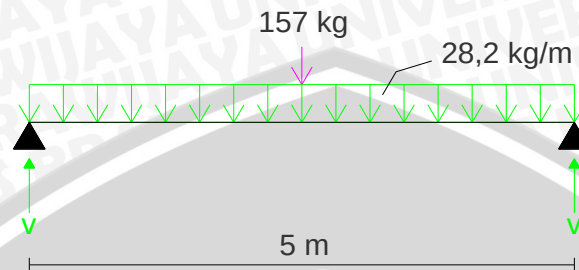
Kombinasi terhadap Sumbu- y

Kombinasi	M.D		M.La		M_y (kgm)
1	1,4	2		=	2
2	1,2	2		0,5 9	= 6
3	1,2	2	+	1,6 9	= 16
4	1,2	2	+	0,5 9	= 6
5	1,2	2		=	2
6	0,9	2		=	2
M_y MAX					= 16

Berdasarkan perhitungan di atas, kombinasi pembebanan yang dipakai untuk mendesain gording adalah kombinasi 3, yaitu 1,2 D + 1,6 La.

$$1,2 D = 1,2 \times 24 = 28,2 \text{ kg/m}$$

$$1,6 La = 1,6 \times 98 = 157 \text{ kg}$$



Reaksi beban (V) berdasarkan pembebanan di atas dapat dihitung melalui,

$$\begin{aligned} V &= 0,5 \times (157 + 28,2 \cdot 5) \\ &= 149 \text{ kg} \end{aligned}$$

sedangkan momen pada $\frac{1}{4}$ bentang, $\frac{3}{4}$ bentang dan $\frac{1}{2}$ bentang berturut-turut,

$$\begin{aligned} M_{1/4L} &= M_{3/4L} = V \cdot 0,25 L - 0,5 \cdot q \cdot (0,25 L)^2 \\ &= 149 \cdot 0,25 \cdot 5 - 0,5 \cdot 28,2 \cdot (0,25 \cdot 5)^2 \\ &= 164 \text{ kgm} \end{aligned}$$

$$\begin{aligned} M_{\max} &= M_{1/2L} = V \cdot 0,5 L - 0,5 \cdot q \cdot (0,5 L)^2 \\ &= 149 \cdot 0,5 \cdot 5 - 0,5 \cdot 28,2 \cdot (0,5 \cdot 5)^2 \\ &= 284 \text{ kgm} \end{aligned}$$

A.3 Kontrol Desain

Lendutan terbesar untuk pembebanan gording tersebut,

$$EI = 2000000 \frac{\text{kg}}{\text{cm}^2} \times 332 \text{ cm}^4$$

$$= 664000000 \text{ kgcm}^2$$

$$= 66400 \text{ kgm}^2$$

$$\theta_{0,5L} = \frac{1}{EI} \int -M_{\max} dx$$

$$= \frac{1}{EI} \int_0^{0,5L} - \left(V \cdot x - \frac{1}{2} q x^2 \right) dx$$

$$= \frac{1}{EI} \int_0^{2,5} -149 \cdot x + \frac{1}{2} 28,2 x^2 dx$$

$$= \frac{1}{EI} \left[-\frac{149 \cdot x^2}{2} + \frac{1}{2} \cdot \frac{1}{3} 28,2x^3 + c_1 \right]_0^{2,5}$$

$$= \frac{1}{EI} \left(-\frac{149 \cdot 2,5^2}{2} + \frac{1}{2} \cdot \frac{1}{3} 28,2 \cdot 2,5^3 + c_1 \right)$$

$$0 = -391,2 + c_1$$

$$c_1 = 391,2$$

$$\Delta_{max} = \frac{1}{EI} \int \theta_{0,5L} dx$$

$$= \frac{1}{EI} \int_0^{2,5} -\frac{149 \cdot x^2}{2} + \frac{1}{2} \cdot \frac{1}{3} 28,2x^3 + c_1 dx$$

$$= \frac{1}{EI} \left[-\frac{149 \cdot x^3}{2 \cdot 3} + \frac{1}{6} \cdot \frac{1}{4} 28,2x^4 + c_1x + c_2 \right]_0^{2,5}$$

$$= \frac{1}{EI} \left[-\frac{149 \cdot x^3}{6} + \frac{1}{24} 28,2x^4 + 391,2x + c_2 \right]_0^{2,5} \rightarrow c_2 = 0$$

$$= \frac{1}{EI} \left(-\frac{149 \cdot 2,5^3}{6} + \frac{1}{24} 28,2 \cdot 2,5^4 + 391,2 \cdot 2,5 \right)$$

$$\Delta_{max} = \frac{636,7}{EI} m$$

$$= \frac{509,4}{66400} m$$

$$= 0,00959 m = 9,59 mm$$

Batas-batas lendutan untuk keadaan kemampuan-layan batas harus sesuai dengan struktur, fungsi penggunaan, sifat pembebanan, serta elemen-elemen yang didukung oleh struktur tersebut (Anonymous, 2000:15). Batas lendutan untuk balok yang memikul lentur adalah $L/240 = 5/240 = 0,02083 m = 20,83 mm$, sehingga lendutan gording aman.

Kontrol kelangsingan profil

Untuk Sayap

$$\lambda = \frac{bf}{tf} = \frac{65}{3,2} = 20,3125$$

$$\lambda_p = \frac{170}{f_y^{0.5}} = \frac{170}{240^{0.5}} = 10,973453$$

Fr = 70 MPA untuk penampang di rol (SNI 2002, tabel 7.5-1)

$$\lambda_r = \frac{370}{(f_y - Fr)^{0.5}} = \frac{370}{(240 - 70)^{0.5}} = 28,377705$$

jika, $\lambda > \lambda_p < \lambda_r$ **Penampang tidak kompak**

Untuk Badan

$$\lambda = \frac{h}{tw} = \frac{150}{3,2} = 46,875$$

$$\lambda_p = \frac{1680}{f_y^{0.5}} = \frac{1680}{240^{0.5}} = 108,44353$$

$$\lambda_r = \frac{2550}{(f_y - Fr)^{0.5}} = \frac{2550}{(240 - 70)^{0.5}} = 195,57607$$

jika, $\lambda < \lambda_p < \lambda_r$ **Penampang kompak**

Penampang kompak untuk badan, maka :

$$\begin{aligned} M_n = M_p &= f_y \times 1,5 \times S_x \\ &= 2400 \times 1,5 \times 44,3 \\ &= 159480 \text{ kg.cm} = 1594,8 \text{ kg.m} \end{aligned}$$

Penampang tidak kompak untuk sayap, maka :

$$M_n = M_p - (M_p - M_r) \frac{\lambda - \lambda_p}{\lambda_r - \lambda_p} = 1143,1 \text{ kg.m}$$

Kontrol Momen (SNI 03-1729-2002, pasal 8.2 - 1.a)

ϕ	M_n	$\geq$	M_u	
0,9	1143,1	$\geq$	284	
	1028,8	$\geq$	284	(kg.m) Ok

Kuat Nominal Lentur

Kuat Nominal Lentur Penampang dengan pengaruh tekuk lateral (SNI 03-1729-2002 pasal 8.3.1)

$$J = 1/3 \cdot (\sum (\text{panjang tebal})^3 = 1/3 \sum (b \cdot t^3)$$

$$J = \text{konstanta puntir torsi (mm}^4)$$

$$J = 1/3 (2 \cdot 6,5 \cdot 0,32^3 + 15 \cdot 0,32^3 + 0,32 \cdot 2^3)$$

$$J = 361,8 \text{ cm}^4$$

$$x_1 = \frac{\pi}{S_x} \sqrt{\frac{E.G.J.A}{2}} = \frac{\pi}{115} \sqrt{\frac{2.10^6 \cdot 8.10^5 \cdot 19281252371}{2}} = 3732008 \text{ kg/cm}^2$$

$$I_w = \frac{I_y \cdot h^2}{4} = \frac{53,8}{4} \cdot 15^2 = 3026,25 \text{ cm}^6$$

$$x_2 = 4 \cdot \left(\frac{S_x}{G.J} \right)^2 \frac{I_w}{I_y} = 4 \cdot \left(\frac{44,3}{8,00E+05 \cdot 361,8487} \right)^2 \cdot \frac{3026,25}{53,8} = 5,26934E-12 \text{ cm}^2/\text{kg}$$

$$L_p = 1,76 \cdot r_y \cdot \sqrt{\frac{E}{f_y}} = 1,76 \cdot 2,37 \cdot \sqrt{\frac{2000000}{2400}} \cdot 0,5 = 120,412 \text{ cm} \quad (\text{SNI 03-1729-2002, tabel 8.3 - 2})$$

$$L_r = \frac{r_y \cdot X_1}{f_y - F_r} \sqrt{1 + \sqrt{1 + X_2 (f_y - F_r)^2}} \quad (\text{SNI 03-1729-2002, tabel 8.3 - 2})$$

$$= \frac{7,28 \times 1719294}{3200 - 700} \sqrt{1 + \sqrt{1 + 7,999710^{-7} (3200 - 700)^2}} = 7357,9539 \text{ cm}$$

(SNI 03-1729-2002, pasal. 8.3.4)

$L_p < L < L_r$ Bentang Menengah

$$C_b = \frac{12,5 M_{\max}}{2,5 M_{\max} + 3M_a + 4M_b + 3M_c}$$

$$M_a = 163,81496$$

$$M_c = 163,81496$$

$$C_b = 1,25$$

$$\begin{aligned} M_p &= f_y \times Z_x \quad (Z_x = 1,5 S_x) \\ &= 2400 \times 1,5 \times 44,3 \\ &= 159480 \text{ kg.cm} \\ &= 1594,8 \text{ kg.m} \end{aligned}$$

$$\begin{aligned} M_r &= (f_y - f_r) S_x \\ &= 1700 \times 44,3 \\ &= 75310 \text{ kg.cm} \\ &= 753,1 \text{ kg.m} \end{aligned}$$

$$M_n = C_b \left[M_r + (M_p - M_r) \frac{L_r - L_b}{L_r - L_p} \right] \leq M_p \text{ (SNI 03-1729-2002, pasal. 8.3.-1)}$$

$$= 1,25 \left[753,1 + 841,7 \frac{6857,954}{7237,54} \right]$$

$$= 1945 \text{ kgm} > 1595 \text{ dipakai } M_p$$

Sehingga di pake $M_p = 1595 \text{ kg.m}$

ϕ	M_n	$\geq$	M_u	
0,9	1595	$\geq$	284	
	1435	$\geq$	284	(kg.m) Ok

Profil kuat menahan momen terhadap tekuk lateral



Lampiran 5. Perencanaan Trekstang

B. Perencanaan Trekstang

B.1 Data perencanaan

Trekstang digunakan untuk mengurangi lendutan gording searah sumbu-x. Trekstang direncanakan sebagai batang tarik karena penampangnya memiliki inersia kecil. Data-data yang dipergunakan dalam perhitungan trekstang ini adalah:

- Mutu baja tulangan
 $f_y = 240 \text{ MPa}$
 $f_u = 370 \text{ MPa}$
- Profil gording yang dipakai Light Lip Channels 150.65.20.3,2
 berat profil = 7,51 kg/m
 jumlah gording pada 1 sisi atap = 14 buah
- Jarak antar gording = 1,3 m
- Jarak trekstang = jarak antar kuda-kuda / 3
 $= 5 / 3$
 $= 1,67 \text{ m}$
- berat air hujan = 20 kg/m^2
- berat sendiri penutup atap = 11 kg/m^2

B.2 Beban pada Trekstang

Beban pada trekstang antara lain:

a) Beban mati (P_D)

Beban mati ini terdiri atas berat sendiri gording dan berat penutup atap.

- Berat gording = berat sendiri profil x jarak trekstang
 $= 7,51 \times 1,67$
 $= 12,52 \text{ kg}$
- Berat penutup atap = berat sendiri x jarak trekstang x jarak gording
 $= 11 \times 1,67 \times 1,3$
 $= 23,83 \text{ kg}$
- Total beban mati = $P_D = \text{berat gording} + \text{berat penutup atap}$

$$= 12,52 + 23,83$$

$$= 36,35 \text{ kg}$$

b) Beban pekerja (P_{La}) = 100 kg

c) Beban air hujan (P_H) = berat air hujan x jarak trekstang x jarak gording

$$= 20 \times 1,67 \times 1,3$$

$$= 43,33 \text{ kg}$$

D	La	P_u (kg)
1,4	36,35	= 51
1,2	36,35 + 0,5	= 94
1,2	36,35 + 1,6	= 204
1,2	36,35 + 0,5	= 94
1,2	36,35	= 44
0,9	36,35	= 33
P MAX		= 204

Berdasarkan tabel di atas, kombinasi beban terbesar adalah 204 kg, maka gaya tarik searah trekstang yang terjadi adalah

$$P = P_u \times \sin 12^\circ$$

$$= 204 \times \sin 12^\circ$$

$$= 42,33 \text{ kg}$$

B.3 Kontrol Desain

Komponen struktur yang memikul gaya tarik aksial terfaktor N_u harus memenuhi $N_u \leq \phi N_n$ (Anonymus, 2000: 70) dengan $\phi = 0,9$ untuk keruntuhan leleh dan $\phi = 0,75$ untuk keruntuhan tarik. Berdasarkan keruntuhan leleh, diameter tulangan trekstang yang dibutuhkan adalah

$$N_u = \text{jumlah gording 1 sisi} \times P$$

$$= 14 \times 42,33$$

$$= 592,69 \text{ kg}$$

$$N_u \leq \phi f_y A_g$$

$$592,69 \leq 0,9 \times 2400 \times 0,25 \pi d^2$$

$$0,349 \leq d^2$$

$$0,591 \leq d$$

berdasarkan keruntuhan tarik,

$$N_u \leq \phi f_u A_e$$

$$592,69 \leq 0,75 \times 3700 \times 0,25 \pi d^2$$

$$0,272 \leq d^2$$

$$0,521 \leq d$$

agar memenuhi seluruh kebutuhan tulangan berdasarkan keruntuhan tarik dan keruntuhan leleh, maka digunakan baja tulangan dengan diameter 6 mm.

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Lampiran 6. Perencanaan Struktur Portal

C.1 Data perencanaan & spesifikasi profil portal

Data-data yang digunakan untuk merencanakan struktur portal ini antara lain:

–	E	= 200000 Mpa	
–	f_r	= 70	Mpa
–	f_y	= 240	Mpa
–	G	= 80000	MPa

Profil yang dipakai: WF 400.200.8.13

–	d	= 400	mm
–	b	= 200	mm
–	Luas penampang = 8412 mm ²		
–	Berat	= 66	kg/m
–	t_f	= 13	mm
–	t_w	= 8	mm
–	I_y	= 53,8	cm ⁴
–	r	= 16	mm
–	S_x	= 44,3	cm ³
–	r_x	= 5,89	cm
–	r_y	= 2,37	cm

C.2 Beban Portal

Kombinasi pembebanan untuk struktur baja bangunan gedung berdasarkan SNI 03-1729-2002, antara lain:

1. $1,4D$
2. $1,2D + 1,6L + 0,5(L_a \text{ atau } H)$
3. $1,2D + 1,6(L_a \text{ atau } H) + (\gamma_L L \text{ atau } 0,8W)$
4. $1,2D + 1,3W + \gamma_L L + 0,5(L_a \text{ atau } H)$
5. $1,2D \pm 1,0E + \gamma_L L$
6. $0,9D \pm (1,3W \text{ atau } 1,0E)$

Keterangan:

D adalah beban mati yang diakibatkan oleh berat konstruksi permanen, termasuk dinding, lantai, atap, plafon, partisi tetap, tangga, dan peralatan tetap

- L adalah beban hidup yang ditimbulkan oleh penggunaan gedung, termasuk kejut, tetapi tidak termasuk beban lingkungan seperti angin, hujan, dan lain-lain
- L_a adalah beban hidup di atap yang ditimbulkan selama perawatan oleh pekerja, peralatan, dan material, atau selama penggunaan biasa oleh orang dan benda bergerak
- H adalah beban hujan, tidak termasuk yang diakibatkan genangan air
- W adalah beban angin
- E adalah beban gempa, yang ditentukan menurut SNI 03-1726-1989, atau penggantinya

Beban yang terdapat dalam perencanaan struktur bangunan ini adalah beban mati (D), beban hidup akibat pekerja (L_a), beban air hujan (H) dan beban angin (W). Kombinasi pembebanan 1 dan 5, 4 dan 6 identik, sehingga diambil yang terbesar sehingga diambil kombinasi pembebanan 1 dan 4.

a) Beban Mati (D)

- Berat sendiri kuda-kuda + alat sambung (10% berat profil kuda-kuda)

$$= 66 + 6,6$$

$$= 73 \text{ kg/m}$$
- Berat penutup atap

$$= \text{Berat sendiri penutup atap} \times \text{jarak antar kuda-kuda} \times \text{jarak antar gording}$$

$$= 11 \times 5 \times 1,3$$

$$= 72 \text{ kg}$$
- Berat gording

$$= \text{Berat gording} \times \text{jarak antar kuda-kuda}$$

$$= 7,51 \times 5$$

$$= 38 \text{ kg}$$
- Berat sendiri kolom

$$= \text{Berat kolom} \times \text{panjang kolom}$$

$$= 66 \times 7,5$$

$$= 495 \text{ kg}$$
- Beban mati terpusat total = **604 kg**

b) Beban hidup akibat pekerja (L_a)

Beban hidup pada atap dan atau pada bagian atap serta pada struktur tudung (canopi) yang dapat dipakai dan dibebani oleh orang harus diambil minimum sebesar 100 kg bidang datar (PPIUG 1983 pasal 3.2.1).

$$P_{La} = 100 \text{ kg}$$

c) Beban air hujan (H)

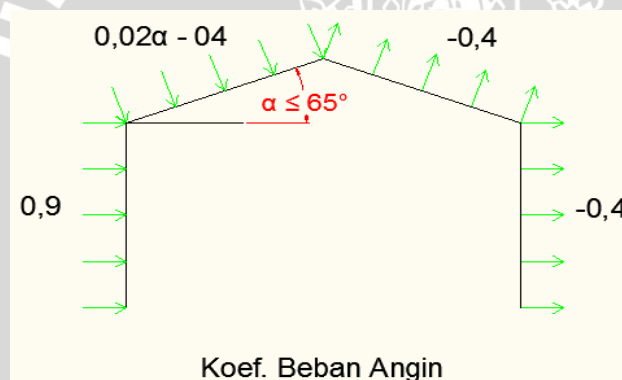
Beban terbagi rata per m^2 bidang datar berasal dari beban air hujan sebesar $(40-0,8\alpha)$ kg/m^2 (**PPIUG 1983 pasal 3.2.2.a**).

$$\begin{aligned} W_a &= 40 - 0,8 \times \alpha \\ &= 40 - 0,8 \times 12 \\ &= 30,4 \text{ kg/m}^2 \text{ (tidak perlu diambil lebih besar dari } 20 \text{ kg/m}^2\text{)} \end{aligned}$$

$$\begin{aligned} W_a \text{ pakai} &= 20 \text{ kg/m}^2 \\ H &= W_a \times \text{jarak antar kuda-kuda} \times \text{jarak gording} \\ &= 20 \times 5 \times 1,3 \\ &= 130 \text{ kg} \end{aligned}$$

Beban hidup akibat pekerja (L_a) dan beban air hujan (H) dipakai yang terbesar yaitu beban air hujan (H) sebesar 130 kg.

d) Beban Angin (W)



Sumber: PPIUG 1983 pasal 4.3

Tekanan angin minimum 25 kg/m^2 untuk daerah yang jauh dari tepi pantai

$$\begin{aligned} c_1 &= \text{koef. Angin tekan atap} \\ &= 0,02 \times \alpha - 0,4 \\ &= 0,02 \times 12 - 0,4 \\ &= -0,16 \\ c_2 &= \text{koef. Angin hisap atap} \\ &= -0,4 \\ c_3 &= \text{koef. Angin tekan dinding} \\ &= 0,9 \\ c_4 &= \text{koef. Angin hisap dinding} \\ &= -0,4 \end{aligned}$$

- Beban angin pada atap
 - $q \text{ tekan} = c_1 \times 25 \times \text{jarak antar kuda-kuda} \times \cos \alpha$
 - $= -20 \text{ kg/m}$
 - $q \text{ hisap} = c_2 \times 25 \times \text{jarak antar kuda-kuda} \times \cos \alpha$
 - $= -49 \text{ kg/m}$
- Beban angin pada dinding
 - $q \text{ tekan} = c_3 \times 25 \times \text{jarak antar kuda-kuda}$
 - $= 113 \text{ kg/m}$
 - $q \text{ hisap} = c_4 \times 25 \times \text{jarak antar kuda-kuda}$
 - $= -50 \text{ kg/m}$

- **Kombinasi Pembebanan Portal**

- Beban-beban pada portal

a) $q_D = 73 \text{ kg/m}$

b) $P_D:$

Penutup atap	=	72	
gording	=	38	+
		109	kg

Penutup atap	=	72	
2 x gording	=	75	+
		147	kg

Penutup atap	=	72	
gording	=	38	
kolom	=	495	+
		604	kg

c) $La = 100 \text{ kg}$

d) $H = 130 \text{ kg}$

e) W

pada atap	=	-20	kg/m	(diabaikan karena memperingan struktur)
pada kolom	=	113	kg/m	

TABEL DATA BATANG

$$A = 84,12 \text{ cm}^2$$

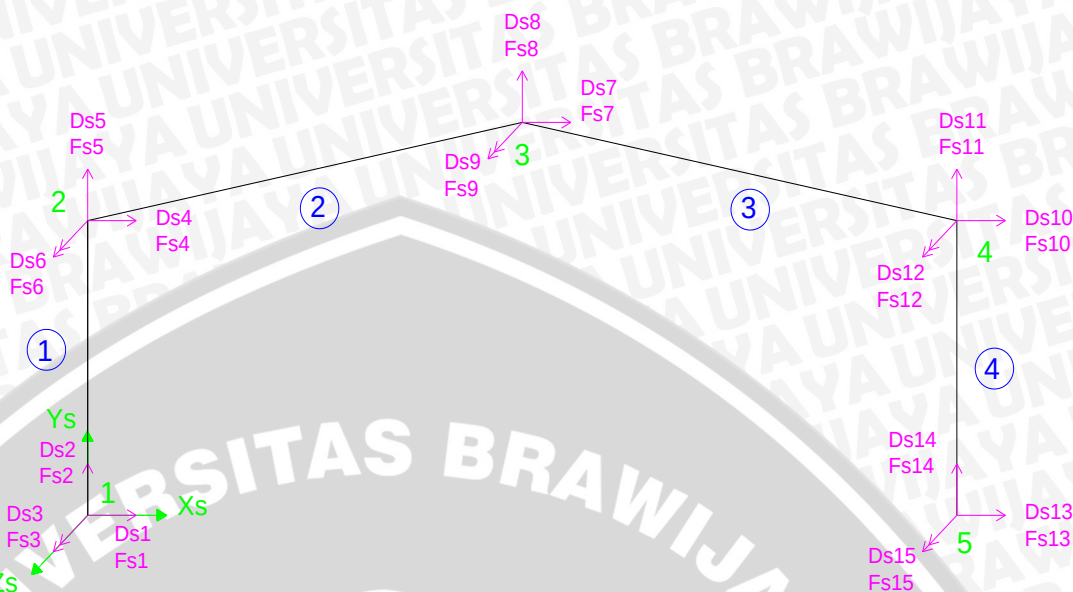
$$E = 2000000 \text{ kg/cm}^2$$

$$I_x = 23700 \text{ cm}^4$$

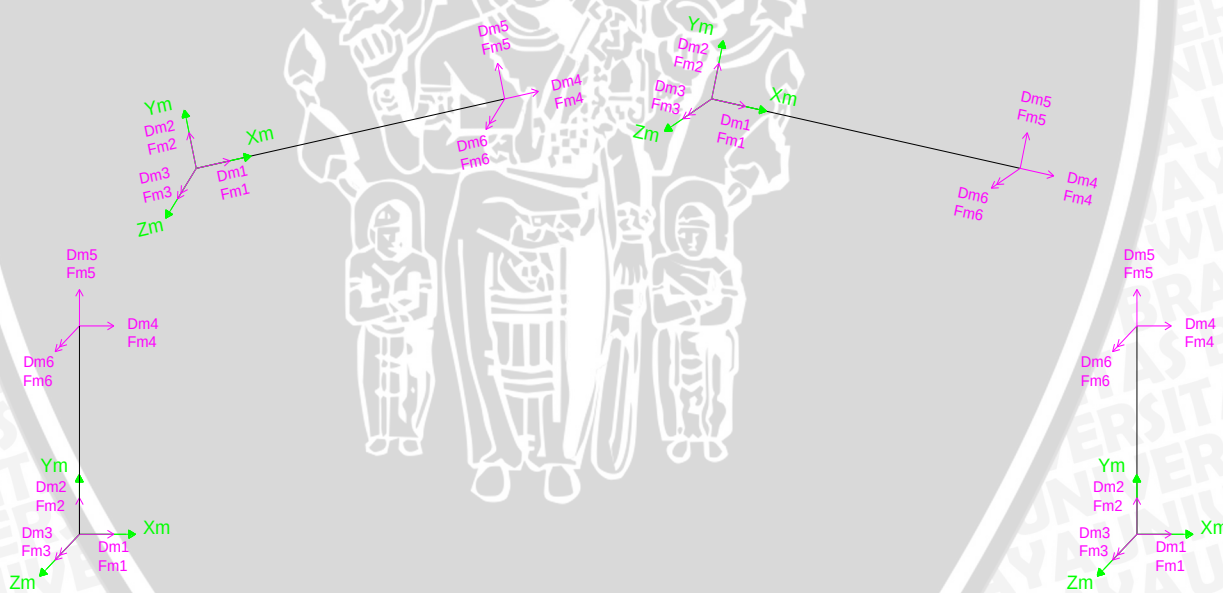
No. Btg	Nomor Titik		L (m)	Sudut α	Cos α	Sin α	EA/L (kg/m)	$12EI/L^3$ (kg/m)	$6EI/L^2$ (kg)	$4EI/L$ (kgm)	$2EI/L$ (kgm)
	i	j									
1	1	2	7,5	90	0	1	22432000	134827	505600	2528000	1264000
2	2	3	15,7	12	0,978	0,208	10720753	14718	115484	1208188	604094
3	3	4	15,7	348	0,978	-0,208	10720753	14718	115484	1208188	604094
4	4	5	7,5	270	0	-1	22432000	134827	505600	2528000	1264000



SISTEM KOORDINAT GLOBAL (SKG)



SISTEM KOORDINAT LOKAL (SKL)



• MATRIKS KEKAKUAN BATANG PADA SUMBU BATANG (XM-YM-ZM)

Rumus Umum

$$[Sm]_i = \begin{pmatrix} EA/L & 0 & 0 & -EA/L & 0 & 0 \\ 0 & 12EI/L^3 & 6EI/L^2 & 0 & -12EI/L^3 & 6EI/L^2 \\ 0 & 6EI/L^2 & 4EI/L & 0 & -6EI/L^2 & 2EI/L \\ -EA/L & 0 & 0 & EA/L & 0 & 0 \\ 0 & -12EI/L^3 & -6EI/L^2 & 0 & 12EI/L^3 & -6EI/L^2 \\ 0 & 6EI/L^2 & 2EI/L & 0 & -6EI/L^2 & 4EI/L \end{pmatrix}$$

$$[Sm]_1 = \begin{pmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{pmatrix}$$

$$[Sm]_2 = \begin{pmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{pmatrix}$$

$$[Sm]_3 = \begin{pmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{pmatrix}$$

$$[Sm]_4 = \begin{pmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{pmatrix}$$

• MATRIKS ROTASI TRANSFORMASI

Rumus Umum

$$[RT]_i = \begin{pmatrix} \cos \alpha & \sin \alpha & 0 & 0 & 0 & 0 \\ -\sin \alpha & \cos \alpha & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & \cos \alpha & \sin \alpha & 0 \\ 0 & 0 & 0 & -\sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$[RT]_1 = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$[RT]_2 = \begin{pmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$[RT]_3 = \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$[RT]_4 = \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

• MATRIKS ROTASI TRANSFORMASI TRANSPOSE

Rumus Umum

$$[RT]^T_1 = \begin{pmatrix} \cos \alpha & -\sin \alpha & 0 & 0 & 0 & 0 \\ \sin \alpha & \cos \alpha & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & \cos \alpha & -\sin \alpha & 0 \\ 0 & 0 & 0 & \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$[RT]^T_1 = \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$[RT]^T_2 = \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$[RT]^T_3 = \begin{pmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$[RT]^T_4 = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

(Berdasarkan sumbu struktur)

[Ss]	=	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
	1	134827	0	-505600	-134827	0	-505600	0	0	0	0	0	0	0	0	0
	2	0	22432000	0	0	-22432000	0	0	0	0	0	0	0	0	0	0
	3	-505600	0	2528000	505600	0	1264000	0	0	0	0	0	0	0	0	0
	4	-134827	0	505600	10392787	2177268	481590	-10257960	-2177268	-24010	0	0	0	0	0	0
	5	0	-22432000	0	2177268	22909511	112960	-2177268	-477511	112960	0	0	0	0	0	0
	6	-505600	0	1264000	481590	112960	3736188	24010	-112960	604094	0	0	0	0	0	0
	7	0	0	0	-10257960	-2177268	24010	20515920	0	48021	-10257960	2177268	24010	0	0	0
	8	0	0	0	-2177268	-477511	-112960	0	955021	0	2177268	-477511	112960	0	0	0
	9	0	0	0	-24010	112960	604094	48021	0	2416375	-24010	-112960	604093,76	0	0	0
	10	0	0	0	0	0	0	-10257960	2177268	-24010	10392787	-2177268	481590	-134827	0	505600
	11	0	0	0	0	0	0	2177268	-477511	-112960	-2177268	22909511	-112960	0	-22432000	0
	12	0	0	0	0	0	0	24010	112960	604094	481590	-112960	3736188	-505600	0	1264000
	13	0	0	0	0	0	0	0	0	0	-134827	0	-505600	134827	0	-505600
	14	0	0	0	0	0	0	0	0	0	0	-22432000	0	0	22432000	0
	15	0	0	0	0	0	0	0	0	0	505600	0	1264000	-505600	0	2528000

• **Introduksi Kondisi Batas Pada Persamaan Global**

Rumus: $\{Fs\} = [Ss] \cdot \{Ds\}$

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15		
F1	134827	0	-505600	-134827	0	-505600	0	0	0	0	0	0	0	0	0	1	x Ds1
F2	0	22432000	0	0	-22432000	0	0	0	0	0	0	0	0	0	0	2	Ds2
F3	-505600	0	2528000	505600	0	1264000	0	0	0	0	0	0	0	0	0	3	Ds3
F4	-134827	0	505600	10392787	2177268	481590	-10257960	-2177268	-24010	0	0	0	0	0	0	4	Ds4
F5	0	-22432000	0	2177268	22909511	112960	-2177268	-477511	112960	0	0	0	0	0	0	5	Ds5
F6	-505600	0	1264000	481590	112960	3736188	24010	-112960	604094	0	0	0	0	0	0	6	Ds6
F7	0	0	0	-10257960	-2177268	24010	20515920	0	48021	-10257960	2177268	24010	0	0	0	7	Ds7
F8	0	0	0	-2177268	-477511	-112960	0	955021	0	2177268	-477511	112960	0	0	0	8	Ds8
F9	0	0	0	-24010	112960	604094	48021	0	2416375	-24010	-112960	604094	0	0	0	9	Ds9
F10	0	0	0	0	0	0	-10257960	2177268	-24010	10392787	-2177268	481590	-134827	0	505600	10	Ds10
F11	0	0	0	0	0	0	2177268	-477511	-112960	-2177268	22909511	-112960	0	-22432000	0	11	Ds11
F12	0	0	0	0	0	0	24010	112960	604094	481590	-112960	3736188	-505600	0	1264000	12	Ds12
F13	0	0	0	0	0	0	0	0	0	-134827	0	-505600	134827	0	-505600	13	Ds13
F14	0	0	0	0	0	0	0	0	0	0	-22432000	0	0	22432000	0	14	Ds14
F15	0	0	0	0	0	0	0	0	0	505600	0	1264000	-505600	0	2528000	15	Ds15

• Penataan Ulang Persamaan Global

	4	5	6	7	8	9	10	11	12	1	2	3	13	14	15		
F4	=	10392787	2177268	481590	-10257960	-2177268	-24010	0	0	0	-134827	0	505600	0	0	0	4 x Ds4
F5		2177268	22909511	112960	-2177268	-477511	112960	0	0	0	0	-22432000	0	0	0	0	5 Ds5
F6		481590	112960	3736188	24010	-112960	604094	0	0	0	-505600	0	1264000	0	0	0	6 Ds6
F7		-10257960	-2177268	24010	20515920	0	48021	-10257960	2177268	24010	0	0	0	0	0	0	7 Ds7
F8		-2177268	-477511	-112960	0	955021	0	2177268	-477511	112960	0	0	0	0	0	0	8 Ds8
F9		-24010	112960	604094	48021	0	2416375	-24010	-112960	604094	0	0	0	0	0	0	9 Ds9
F10		0	0	0	-10257960	2177268	-24010	10392787	-2177268	-481590	0	0	0	-134827	0	505600	10 Ds10
F11		0	0	0	2177268	-477511	-112960	-2177268	22909511	-112960	0	0	0	0	-22432000	0	11 Ds11
F12		0	0	0	24010	112960	604094	481590	-112960	3736188	0	0	0	-505600	0	1264000	12 Ds12
F1		-134827	0	-505600	0	0	0	0	0	0	134827	0	-505600	0	0	0	1 Ds1
F2		0	-22432000	0	0	0	0	0	0	0	0	22432000	0	0	0	0	2 Ds2
F3		505600	0	1264000	0	0	0	0	0	0	-505600	0	2528000	0	0	0	3 Ds3
F13		0	0	0	0	0	0	-134827	0	-505600	0	0	0	134827	0	-505600	13 Ds13
F14		0	0	0	0	0	0	0	-22432000	0	0	0	0	0	22432000	0	14 Ds14
F15		0	0	0	0	0	0	505600	0	1264000	0	0	0	-505600	0	2528000	15 Ds15

• **Matriks Kekakuan Batang Pada Sumbu Struktur (XS-YS-ZS)**

Rumus: $[Ss]_i = [RT]^T_i \times [Sm]_i \times [RT]_i$

dengan: $[Sm]_i$ = Matriks kekakuan batang pada sumbu batang (SKL)

$[RT]_i$ = Matriks rotasi

$[RT]^T_i$ = Matriks rotasi transpose

$$\begin{aligned}
 [Ss]_1 &= \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134826,6667 & 505600 & 0 & -134826,667 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134826,6667 & -505600 & 0 & 134826,6667 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{pmatrix} \times \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \\
 &= \begin{pmatrix} 134826,67 & 0 & -505600 & -134826,7 & 0 & -505600 \\ 0 & 22432000 & 0 & 0 & -22432000 & 0 \\ -505600 & 0 & 2528000 & 505600 & 0 & 1264000 \\ -134826,67 & 0 & 505600 & 134826,7 & 0 & 505600 \\ 0 & -22432000 & 0 & 0 & 22432000 & 0 \\ -505600 & 0 & 1264000 & 505600 & 0 & 2528000 \end{pmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix} \\
 &\quad \quad \quad \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}
 \end{aligned}$$



$$\begin{aligned}
 [Ss]_2 &= \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{pmatrix} \\
 &\times \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 10257960 & 2177268,294 & -24010,46 & -10257959,9 & -2177268,29 & -24010 \\ 2177268 & 477510,6228 & 112960,3 & -2177268,29 & -477510,623 & 112960 \\ -24010 & 112960,3461 & 1208188 & 24010 & -112960,346 & 604094 \\ -10257960 & -2177268,294 & 24010,46 & 10257959,93 & 2177268,294 & 24010 \\ -2177268 & -477510,6228 & -112960,3 & 2177268 & 477510,6228 & -112960 \\ -24010 & 112960,3461 & 604093,8 & 24010 & -112960,346 & 1208188 \end{pmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix} \\
 [Ss]_3 &= \begin{pmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{pmatrix} \\
 &\times \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 10257960 & -2177268,294 & 24010,46 & -10257959,9 & 2177268,294 & 24010 \\ -2177268 & 477510,6228 & 112960,3 & 2177268,294 & -477510,623 & 112960 \\ 24010 & 112960,3461 & 1208188 & -24010 & -112960,346 & 604094 \\ -10257960 & 2177268,294 & -24010,46 & 10257959,93 & -2177268,29 & -24010 \\ 2177268 & -477510,6228 & -112960,3 & -2177268 & 477510,6228 & -112960 \\ 24010 & 112960,3461 & 604093,8 & -24010 & -112960,346 & 1208188 \end{pmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}
 \end{aligned}$$

$$\begin{aligned}
 [Ss]_4 &= \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{pmatrix} \\
 &\times \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 134827 & 0 & 505600 & -134827 & 0 & 505600 \\ 0 & 22432000 & 0 & 0 & -22432000 & 0 \\ 505600 & 0 & 2528000 & -505600 & 0 & 1264000 \\ -134827 & 0 & -505600 & 134827 & 0 & -505600 \\ 0 & -22432000 & 0 & 0 & 22432000 & 0 \\ 505600 & 0 & 1264000 & -505600 & 0 & 2528000 \end{pmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}
 \end{aligned}$$



- Kombinasi 1**

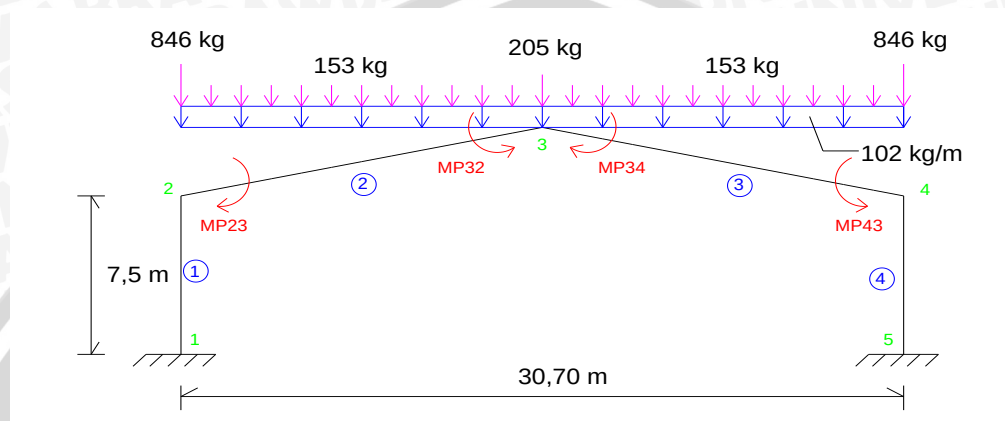
1.4D

$$1,4 q_D = 1,4 \times 73 = 102 \text{ kg/m}$$

$$1,4 P_D: 1,4 \times 109 = 153 \text{ kg}$$

$$1,4 \times 147 = 205 \text{ kg}$$

$$1,4 \times 604 = 846 \text{ kg}$$



Beban	ΣM3		ΣM2	
	Jarak	PxL	Jarak	PxL
102	15,35	11974	15,35	11974
103	0	0	15,35	1575
846	15,35	12981	0	0
153	14,08	2149,4	1,27	194
	12,81	1955,2	2,54	388
	11,54	1761,1	3,81	582
	10,26	1566,9	5,09	777
	8,99	1372,8	6,36	971
	7,72	1178,7	7,63	1165
	6,45	984,55	8,90	1359
	5,18	790,41	10,17	1553
	3,91	596,28	11,44	1747
	2,63	402,15	12,72	1941
	1,36	208,01	13,99	2135
Jumlah		37921	26362	
R2		2470	R3	1717

KONTROL			
102	x	15,35	= 1560
153	x	11	= 1679
205	x	1	= 103
846	x	1	= 846
Jumlah			4188
			4188

OK

- Momen Primer

$$MP_{23} = -MP_{32} = MP_{34} = -MP_{43}$$

$$= \frac{1}{12} qL^2 + \sum \frac{Pab^2}{L^2}$$

c	q	L ²	$\frac{1}{12} qL^2$
$\frac{1}{12}$	102	236	1995,7
P	a	b ²	$\frac{Pab^2}{L^2}$
846	0	236	0
153	1,27	198	163
153	2,54	164	270
153	3,81	133	329
153	5,09	105	347
153	6,36	81	333
153	7,63	60	295
153	8,90	42	240
153	10,17	27	177
153	11,44	15	113
153	12,72	7	57
153	13,99	2	17
205	15,35	0	0
MP23 (kgm)			4337

• **Beban Ekuivalen 1 {Fs}**

$$\{Fs\} = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -2470 \\ -4337 \\ 0 \\ -3435 \\ 0 \\ 0 \\ -2470 \\ 4337 \\ 0 \\ 0 \\ 0 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix} \begin{Bmatrix} F4 \\ F5 \\ F6 \\ F7 \\ F8 \\ F9 \\ F10 \\ F11 \\ F12 \\ F1 \\ F2 \\ F3 \\ F13 \\ F14 \\ F15 \end{Bmatrix} = \begin{Bmatrix} 0 \\ -2470 \\ -4337 \\ 0 \\ -3435 \\ 0 \\ 0 \\ -2470 \\ 4337 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{matrix}$$

Rumus: $\{Ds\} = [Ss]^{-1} \cdot \{Fs\}$

4	5	6	7	8	9	10	11	12					
9,36E-06	3,21E-09	-1,21E-06	8,28E-06	4,91E-06	6,09E-07	7,20E-06	-3,21E-09	-1,23E-06	4	x	0	=	-0,0169
3,21E-09	4,46E-08	-8,55E-10	7,94E-09	2,23E-08	-1,75E-09	3,21E-09	1,57E-12	-8,55E-10	5		-2470		-0,0002
-1,21E-06	-8,55E-10	4,60E-07	-1,22E-06	7,61E-08	-1,62E-07	-1,23E-06	8,55E-10	1,90E-07	6		-4337		-0,0014
8,28E-06	7,94E-09	-1,22E-06	8,33E-06	1,14E-20	6,08E-07	8,28E-06	-7,94E-09	-1,22E-06	7		0		0,0000
4,91E-06	2,23E-08	7,61E-08	7,53E-21	2,35E-05	9,41E-22	-4,91E-06	2,23E-08	-7,61E-08	8		-3435		-0,0813
6,09E-07	-1,75E-09	-1,62E-07	6,08E-07	6,38E-23	4,95E-07	6,09E-07	1,75E-09	-1,62E-07	9		0		0,0000
7,20E-06	3,21E-09	-1,23E-06	8,28E-06	-4,91E-06	6,09E-07	9,36E-06	-3,21E-09	-1,21E-06	10		0		0,0169
-3,21E-09	1,57E-12	8,55E-10	-7,94E-09	2,23E-08	1,75E-09	-3,21E-09	4,46E-08	8,55E-10	11		-2470		-0,0002
-1,23E-06	-8,55E-10	1,90E-07	-1,22E-06	-7,61E-08	-1,62E-07	-1,21E-06	8,55E-10	4,60E-07	12		4337		0,0014

•Kombinasi 1 - Perhitungan Reaksi Tumpuan

Rumus: $\{Fs\} = [Ss] \cdot \{Ds\}$

$$\begin{bmatrix} 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ -134827 & 0 & -505600 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -22432000 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 505600 & 0 & 1264000 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -134827 & 0 & -505600 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -22432000 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 505600 & 0 & 1264000 \end{bmatrix} \times \begin{Bmatrix} 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{Bmatrix} = \begin{Bmatrix} -0,0169 \\ -0,0002 \\ -0,0014 \\ 0,0000 \\ -0,0813 \\ 0,0000 \\ 0,0169 \\ -0,0002 \\ 0,0014 \end{Bmatrix} = \begin{Bmatrix} 3007 \\ 4188 \\ -10371 \\ -3007 \\ 4188 \\ 10371 \end{Bmatrix}$$



•Kombinasi 1 - Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu batang)

$$\text{Rumus: } \{Fm^A\}_i = \{Fm^B\}_i + [Sm]_i \times [RT]_i \times \{Ds\}_i$$

dengan: $\{Fm^A\}_i$ = Gaya dalam batang

$\{Fm^B\}_i$ = Gaya akibat beban luar

$[Sm]_i$ = Matriks kekakuan batang (pada sumbu batang)

$[RT]_i$ = Matriks rotasi

$\{Ds\}_i$ = Perpindahan

$$\{Fm^A\}_1 = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} + \begin{Bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{Bmatrix} \times \begin{Bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0 \\ 0 \\ 0 \\ -0,0169 \\ -0,0002 \\ -0,0014 \end{Bmatrix} = \begin{Bmatrix} 4188 \\ -3007 \\ -10371 \\ -4188 \\ 3007 \\ -12180 \end{Bmatrix}$$

$$\{Fm^A\}_2 = \begin{Bmatrix} 514 \\ 2416 \\ 4337 \\ 357 \\ 1680 \\ -4337 \end{Bmatrix} + \begin{Bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{Bmatrix} \times \begin{Bmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,21 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,21 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} -0,0169 \\ -0,0002 \\ -0,0014 \\ 0,0000 \\ -0,0813 \\ 0,0000 \end{Bmatrix} = \begin{Bmatrix} 3812 \\ 3471 \\ 12180 \\ -2941 \\ 625 \\ 4372 \end{Bmatrix}$$

$$\{Fm^A\}_3 = \begin{Bmatrix} -357 \\ 1680 \\ 4337 \\ -514 \\ 2416 \\ -4337 \end{Bmatrix} + \begin{Bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{Bmatrix} \times \begin{Bmatrix} 0,978 & -0,21 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,21 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0000 \\ -0,0813 \\ 0,0000 \\ 0,0169 \\ -0,0002 \\ 0,0014 \end{Bmatrix} = \begin{Bmatrix} 2941 \\ 625 \\ -4372 \\ -3812 \\ 3471 \\ -12180 \end{Bmatrix}$$

$$\{Fm^A\}_4 = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} + \begin{Bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{Bmatrix} \times \begin{Bmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0169 \\ -0,0002 \\ 0,0014 \\ 0 \\ 0 \\ 0 \end{Bmatrix} = \begin{Bmatrix} 4188 \\ 3007 \\ 12180 \\ -4188 \\ -3007 \\ 10371 \end{Bmatrix}$$



•Kombinasi 1 - Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu struktur)

Rumus: $\{F_s^A\}_i = [RT]^T_i \times \{F_m^A\}_i$

dengan: $\{F_s^A\}_i$ = Gaya dalam akhir batang

$[RT]^T_i$ = Matriks rotasi transpose

$\{F_m^A\}_i$ = Gaya dalam batang

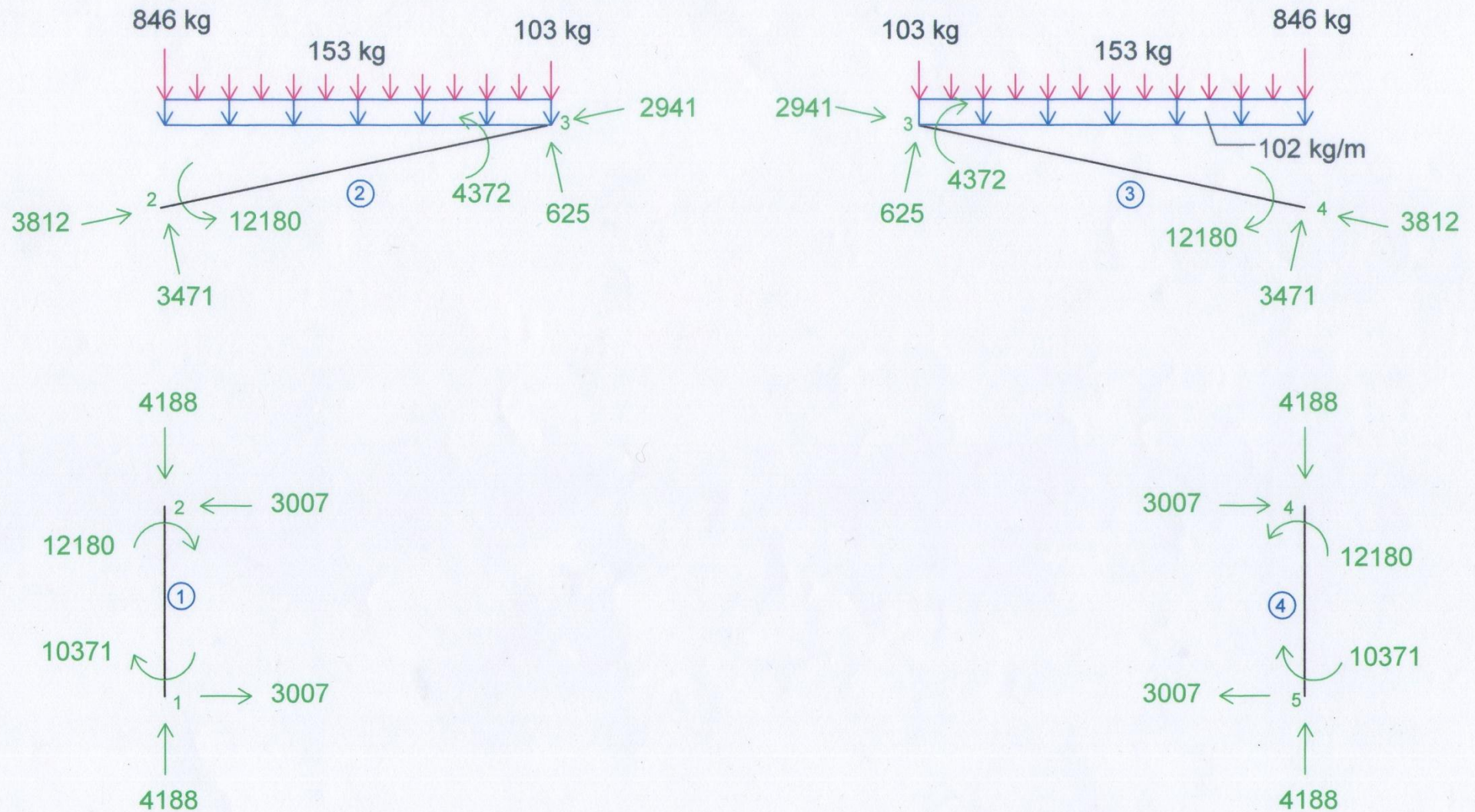
$$\{F_s^A\}_1 = \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4188 \\ -3007 \\ -10371 \\ -4188 \\ 3007 \\ -12180 \end{pmatrix} = \begin{pmatrix} 3007 \\ 4188 \\ -10371 \\ -3007 \\ -4188 \\ -12180 \end{pmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}$$

$$\{F_s^A\}_2 = \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 3812 \\ 3471 \\ 12180 \\ -2941 \\ 625 \\ 4372 \end{pmatrix} = \begin{pmatrix} 3007 \\ 4188 \\ 12180 \\ -3007 \\ 0 \\ 4372 \end{pmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

$$\{F_s^A\}_3 = \begin{pmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 2941 \\ 625 \\ -4372 \\ -3812 \\ 3471 \\ -12180 \end{pmatrix} = \begin{pmatrix} 3007 \\ 0 \\ -4372 \\ -3007 \\ 4188 \\ -12180 \end{pmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\{F_s^A\}_4 = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4188 \\ 3007 \\ 12180 \\ -4188 \\ -3007 \\ 10371 \end{pmatrix} = \begin{pmatrix} 3007 \\ -4188 \\ 12180 \\ -3007 \\ 4188 \\ 10371 \end{pmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$

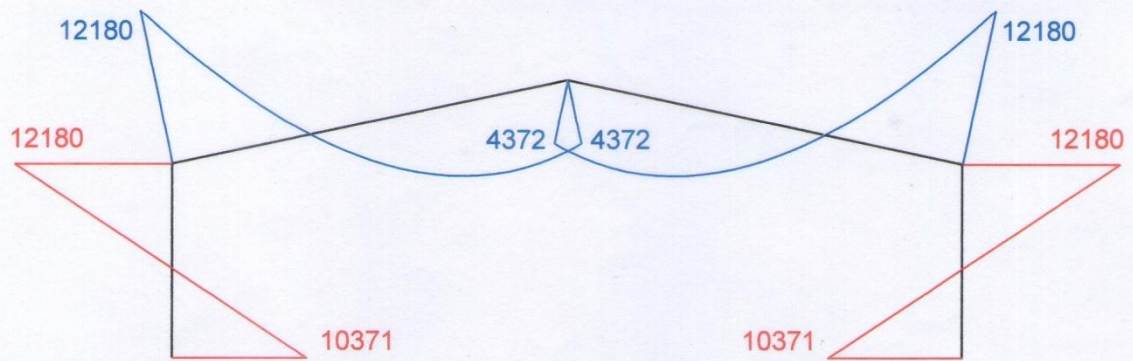
FBD KOMBINASI 1



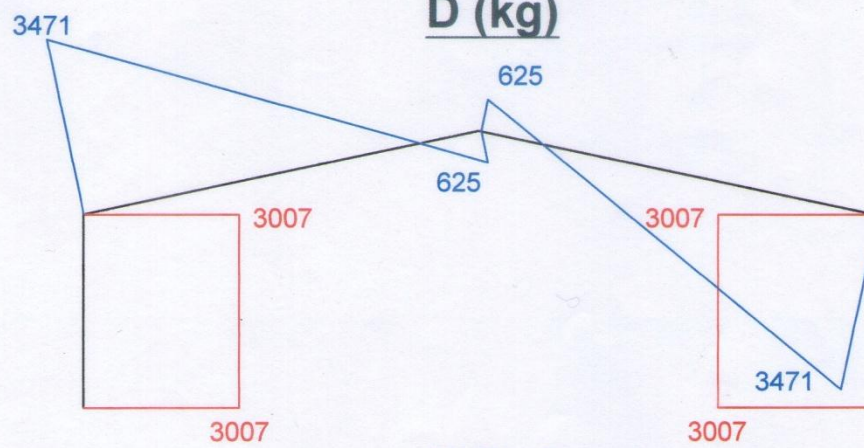
x →	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180
-102	0	-49	-194	-438	-778	-1216	-1750	-2383	-3112	-3938	-4862	-5883	-7002	-8217	-9530	-10842
6 x cos12 = -827	0	-827	-1654	-2482	-3309	-4136	-4963	-5790	-6618	-7445	-8272	-9099	-9926	-10753	-11581	-12408
8 x cos12 = 4096	0	4096	8193	12289	16385	20482	24578	28674	32771	36867	40963	45060	49156	53252	57348	61444
07 x sin12 = -625	0	-625	-1250	-1875	-2501	-3126	-3751	-4376	-5001	-5626	-6252	-6877	-7502	-8127	-8752	-9377
3 x cos12 = -149			-105	-254	-403	-553	-702	-851	-1001	-1150	-1299	-1449	-1598	-1747	-1897	-2046
				-60	-209	-358	-508	-657	-806	-956	-1105	-1254	-1404	-1553	-1702	-1851
					-15	-164	-314	-463	-612	-762	-911	-1060	-1210	-1359	-1508	-1657
							-119	-269	-418	-567	-717	-866	-1015	-1165	-1314	-1463
								-75	-224	-373	-523	-672	-821	-971	-1120	-1269
									-30	-179	-329	-478	-627	-777	-926	-1075
											-134	-284	-433	-582	-732	-881
												-90	-239	-388	-538	-687
													-45	-194	-343	-492
															-149	-298
																-149
Jumlah	-12180	-9585	-7191	-5000	-3010	-1251	290	1630	2768	3690	4379	4867	5154	5238	5076	4758

x →			0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	15,693	
M	-12180		-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	-12180	
q	-102		0	-49	-194	-438	-778	-1216	-1750	-2383	-3112	-3938	-4862	-5883	-7002	-8217	-9530	-10940	-11974	
P	-846	x cos12 = -827	0	-827	-1654	-2482	-3309	-4136	-4963	-5790	-6618	-7445	-8272	-9099	-9926	-10753	-11581	-12408	-12981	
V2	4188	x cos12 = 4096	0	4096	8193	12289	16385	20482	24578	28674	32771	36867	40963	45060	49156	53252	57348	61445	64283	
H2	-3007	x sin12 = -625	0	-625	-1250	-1875	-2501	-3126	-3751	-4376	-5001	-5626	-6252	-6877	-7502	-8127	-8752	-9377	-9811	
1,30	-153	x cos12 = -149			-105	-254	-403	-553	-702	-851	-1001	-1150	-1299	-1449	-1598	-1747	-1897	-2046	-2149	
2,60						-60	-209	-358	-508	-657	-806	-956	-1105	-1254	-1404	-1553	-1702	-1852	-1955	
3,90							-15	-164	-314	-463	-612	-762	-911	-1060	-1210	-1359	-1508	-1658	-1761	
5,20									-119	-269	-418	-567	-717	-866	-1015	-1165	-1314	-1463	-1567	
6,50										-75	-224	-373	-523	-672	-821	-971	-1120	-1269	-1373	
7,80											-30	-179	-329	-478	-627	-777	-926	-1075	-1179	
9,10													-134	-284	-433	-582	-732	-881	-985	
10,40														-90	-239	-388	-538	-687	-790	
11,70															-45	-194	-343	-493	-596	
13,00																		-149	-299	-402
14,30																		-105	-208	
Jumlah			-12180	-9585	-7191	-5000	-3010	-1251	290	1630	2768	3690	4379	4867	5154	5238	5076	4712	4372	
																			Kr(%)	0

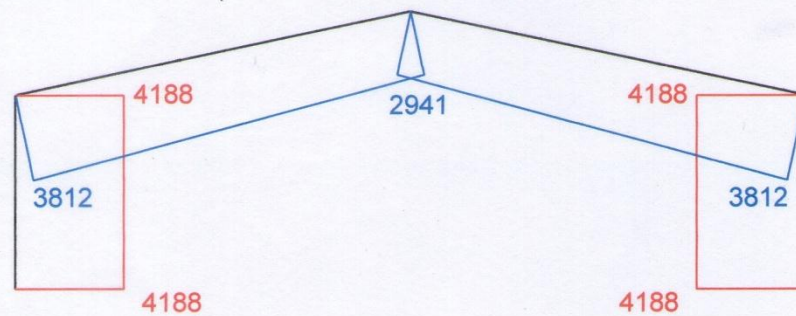
M (kgm)



D (kg)



N (kg)





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Job No

Sheet No

1

Rev

Part

Job Title

Ref

By

Date 12-Mar-13

Chd

Client

File Structure1.std

Date/Time 12-Mar-2013 13:24

Y
Z-X

Load 4 : Bending Z

Whole Structure Mz 1529.57kg-m:1m 4 COMBINATION LOAD CASE 4





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Job No

Sheet No

2

Rev

Part

Job Title

Ref

By

Date 12-Mar-13

Chd

Client

File Structure1.std

Date/Time 12-Mar-2013 13:24

Y
Z-X

Load 4 : Shear Y

Whole Structure Fy 407.886kg:1m 4 COMBINATION LOAD CASE 4



• **Kombinasi 2**

$$1.2D + 1.6L + 0.5(La \text{ atau } H)$$

$La < H \rightarrow$ dipakai H

Kombinasi pembebanannya menjadi:

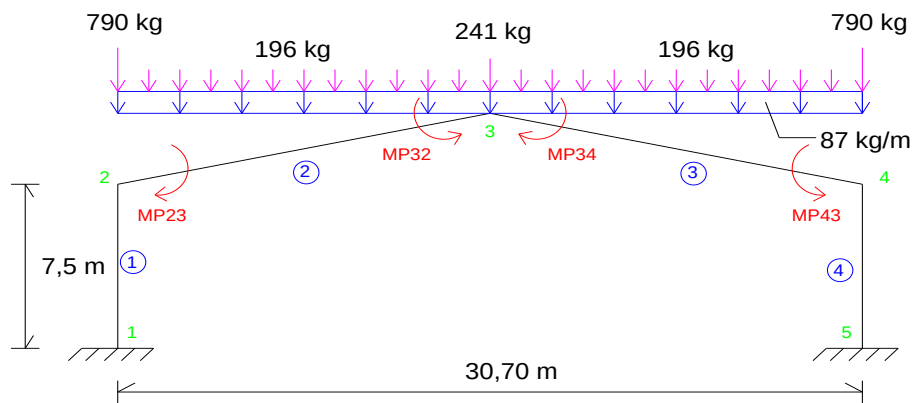
$$1.2D + 0.5H$$

$$1,2 q_D = 1,2 \times 73 = 87 \text{ kg/m}$$

$$1,2 P_D: 1,2 \times 109 + 0,5 \times 130 = 196 \text{ kg}$$

$$1,2 \times 147 + 0,5 \times 130 = 241 \text{ kg}$$

$$1,2 \times 604 + 0,5 \times 130 = 790 \text{ kg}$$



	$\Sigma M3$		$\Sigma M2$	
Beban	Jarak	$P \times L$	Jarak	$P \times L$
87	15,35	10264	15,35	10264
120	0	0	15,35	1849
790	15,35	12124	0	0
196	14,08	2757,4	1,27	249
	12,81	2508,3	2,54	498
	11,54	2259,3	3,81	747
	10,26	2010,2	5,09	996
	8,99	1761,2	6,36	1245
	7,72	1512,1	7,63	1494
	6,45	1263,1	8,90	1743
	5,18	1014	10,17	1992
	3,91	764,97	11,44	2241
	2,63	515,91	12,72	2491
	1,36	266,86	13,99	2740
Jumlah		39021		28550
R2		2542	R3	1860

KONTROL				
87	x	15,35	=	1337
196	x	11	=	2154
241	x	0,5	=	120
790	x	1	=	790
Jumlah				4402
				4402
OK				

- Momen Primer

$$MP_{23} = -MP_{32} = MP_{34} = -MP_{43}$$

$$= \frac{1}{12} qL^2 + \sum \frac{Pab^2}{L^2}$$

c	q	L ²	$\frac{1}{12} qL^2$
$\frac{1}{12}$	87	235,6	1710,6
P	a	b ²	$\frac{Pab^2}{L^2}$
790	0	236	0
196	1,27	198	209
196	2,54	164	347
196	3,81	133	422
196	5,09	105	445
196	6,36	81	427
196	7,63	60	378
196	8,90	42	308
196	10,17	27	227
196	11,44	15	145
196	12,72	7	73
196	13,99	2	22
241	15,35	0	0
MP (kgm)			4714

•Kombinasi 2 - Beban Ekuivalen {Fs}

$$\{Fs\} = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -2542 \\ -4714 \\ 0 \\ -3720 \\ 0 \\ 0 \\ -2542 \\ 4714 \\ 0 \\ 0 \\ 0 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix} \quad \begin{matrix} F4 \\ F5 \\ F6 \\ F7 \\ F8 \\ F9 \\ F10 \\ F11 \\ F12 \\ \hline F1 \\ F2 \\ F3 \\ F13 \\ F14 \\ F15 \end{matrix} = \begin{Bmatrix} 0 \\ -2542 \\ -4714 \\ 0 \\ -3720 \\ 0 \\ 0 \\ -2542 \\ 4714 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{matrix}$$

Rumus: $\{Ds\} = [Ss]^{-1} \cdot \{Fs\}$

4	5	6	7	8	9	10	11	12						
9,36E-06	3,21E-09	-1,21E-06	8,28E-06	4,91E-06	6,09E-07	7,20E-06	-3,21E-09	-1,23E-06	4	x	0	=	-0,0183	m
3,21E-09	4,46E-08	-8,55E-10	7,94E-09	2,23E-08	-1,75E-09	3,21E-09	1,57E-12	-8,55E-10	5		-2542		-0,0002	m
-1,21E-06	-8,55E-10	4,60E-07	-1,22E-06	7,61E-08	-1,62E-07	-1,23E-06	8,55E-10	1,90E-07	6		-4714		-0,0016	rad
8,28E-06	7,94E-09	-1,22E-06	8,33E-06	1,14E-20	6,08E-07	8,28E-06	-7,94E-09	-1,22E-06	7		0		0,0000	m
4,91E-06	2,23E-08	7,61E-08	7,53E-21	2,35E-05	9,41E-22	-4,91E-06	2,23E-08	-7,61E-08	8		-3720		-0,0881	m
6,09E-07	-1,75E-09	-1,62E-07	6,08E-07	6,38E-23	4,95E-07	6,09E-07	1,75E-09	-1,62E-07	9		0		0,0000	rad
7,20E-06	3,21E-09	-1,23E-06	8,28E-06	-4,91E-06	6,09E-07	9,36E-06	-3,21E-09	-1,21E-06	10		0		0,0183	m
-3,21E-09	1,57E-12	8,55E-10	-7,94E-09	2,23E-08	1,75E-09	-3,21E-09	4,46E-08	8,55E-10	11		-2542		-0,0002	m
-1,23E-06	-8,55E-10	1,90E-07	-1,22E-06	-7,61E-08	-1,62E-07	-1,21E-06	8,55E-10	4,60E-07	12		4714		0,0016	rad

•Kombinasi 2 - Perhitungan Reaksi Tumpuan

Rumus: $\{Fs\} = [Ss] \cdot \{Ds\}$

$$\begin{bmatrix} 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ -134827 & 0 & -505600 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -22432000 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 505600 & 0 & 1264000 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -134827 & 0 & -505600 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -22432000 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 505600 & 0 & 1264000 \end{bmatrix} \times \begin{Bmatrix} 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{Bmatrix} = \begin{Bmatrix} -0,0183 \\ -0,0002 \\ -0,0016 \\ 0,0000 \\ -0,0881 \\ 0,0000 \\ 0,0183 \\ -0,0002 \\ 0,0016 \end{Bmatrix} = \begin{Bmatrix} 3259 \\ 4402 \\ -11238 \\ -3259 \\ 4402 \\ 11238 \end{Bmatrix}$$



•Kombinasi 2 - Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu batang)

Rumus: $\{Fm^A\}_i = \{Fm^B\}_i + [Sm]_i \times [RT]_i \times \{Ds\}_i$

dengan: $\{Fm^A\}_i$ = Gaya dalam batang

$\{Fm^B\}_i$ = Gaya akibat beban luar

$[Sm]_i$ = Matriks kekakuan batang (pada sumbu batang)

$[RT]_i$ = Matriks rotasi

$\{Ds\}_i$ = Perpindahan

$$\{Fm^A\}_1 = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} + \begin{Bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{Bmatrix} \times \begin{Bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0 \\ 0 \\ 0 \\ -0,0183 \\ -0,0002 \\ -0,0016 \end{Bmatrix} = \begin{Bmatrix} 4402 \\ -3259 \\ -11238 \\ -4402 \\ 3259 \\ -13203 \end{Bmatrix}$$

$$\{Fm^A\}_2 = \begin{Bmatrix} 529 \\ 2487 \\ 4714 \\ 387 \\ 1819 \\ -4714 \end{Bmatrix} + \begin{Bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{Bmatrix} \times \begin{Bmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,21 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,21 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} -0,0183 \\ -0,0002 \\ -0,0016 \\ 0,0000 \\ -0,0881 \\ 0,0000 \end{Bmatrix} = \begin{Bmatrix} 4103 \\ 3628 \\ 13203 \\ -3188 \\ 678 \\ 4715 \end{Bmatrix}$$

$$\{Fm^A\}_3 = \begin{Bmatrix} -387 \\ 1819 \\ 4714 \\ -529 \\ 2487 \\ -4714 \end{Bmatrix} + \begin{Bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{Bmatrix} \times \begin{Bmatrix} 0,978 & -0,21 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,21 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0000 \\ -0,0881 \\ 0,0000 \\ 0,0183 \\ -0,0002 \\ 0,0016 \end{Bmatrix} = \begin{Bmatrix} 3188 \\ 678 \\ -4715 \\ -4103 \\ 3628 \\ -13203 \end{Bmatrix}$$

$$\{Fm^A\}_4 = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} + \begin{Bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{Bmatrix} \times \begin{Bmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0183 \\ -0,0002 \\ 0,0016 \\ 0 \\ 0 \\ 0 \end{Bmatrix} = \begin{Bmatrix} 4402 \\ 3259 \\ 13203 \\ -4402 \\ -3259 \\ 11238 \end{Bmatrix}$$



•Kombinasi 2 - Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu struktur)

Rumus: $\{F_s^A\}_i = [RT]^T_i \times \{F_m^A\}_i$

dengan: $\{F_s^A\}_i$ = Gaya dalam akhir batang

$[RT]^T_i$ = Matriks rotasi transpose

$\{F_m^A\}_i$ = Gaya dalam batang

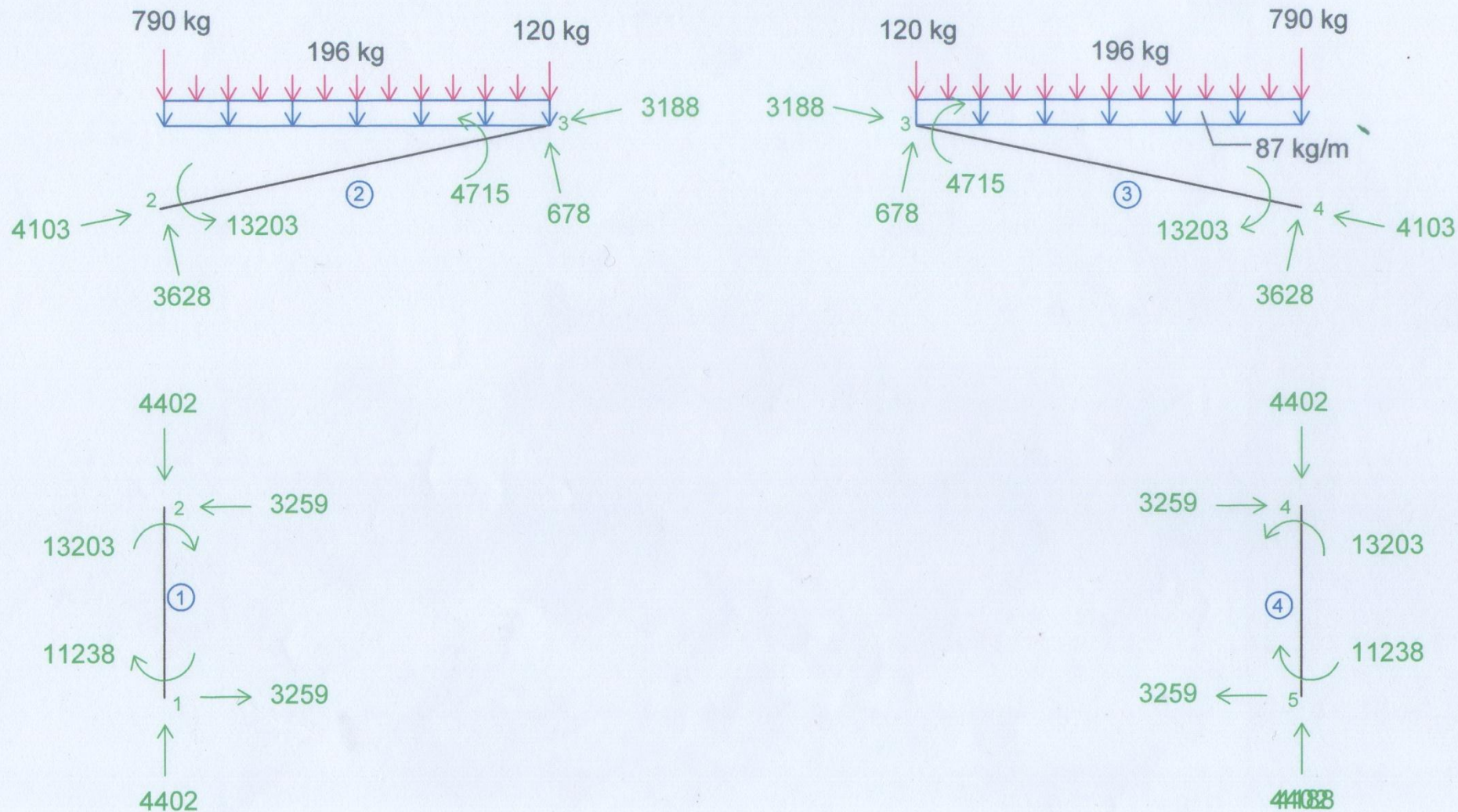
$$\{F_s^A\}_1 = \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4402 \\ -3259 \\ -11238 \\ -4402 \\ 3259 \\ -13203 \end{pmatrix} = \begin{pmatrix} 3259 \\ 4402 \\ -11238 \\ -3259 \\ -4402 \\ -13203 \end{pmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}$$

$$\{F_s^A\}_2 = \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4103 \\ 3628 \\ 13203 \\ -3188 \\ 678 \\ 4715 \end{pmatrix} = \begin{pmatrix} 3259 \\ 4402 \\ 13203 \\ -3259 \\ 0 \\ 4715 \end{pmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

$$\{F_s^A\}_3 = \begin{pmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 3188 \\ 678 \\ -4715 \\ -4103 \\ 3628 \\ -13203 \end{pmatrix} = \begin{pmatrix} 3259 \\ 0 \\ -4715 \\ -3259 \\ 4402 \\ -13203 \end{pmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\{F_s^A\}_4 = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4402 \\ 3259 \\ 13203 \\ -4402 \\ -3259 \\ 11238 \end{pmatrix} = \begin{pmatrix} 3259 \\ -4402 \\ 13203 \\ -3259 \\ 4402 \\ 11238 \end{pmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$

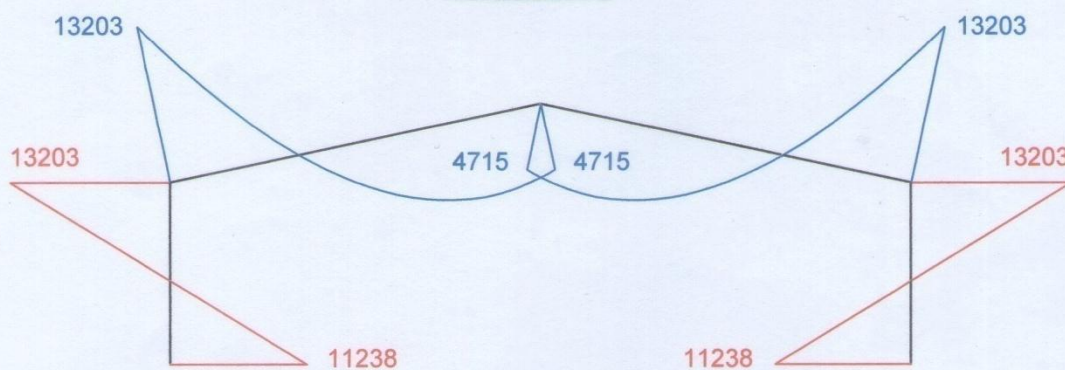
FBD KOMBINASI 2



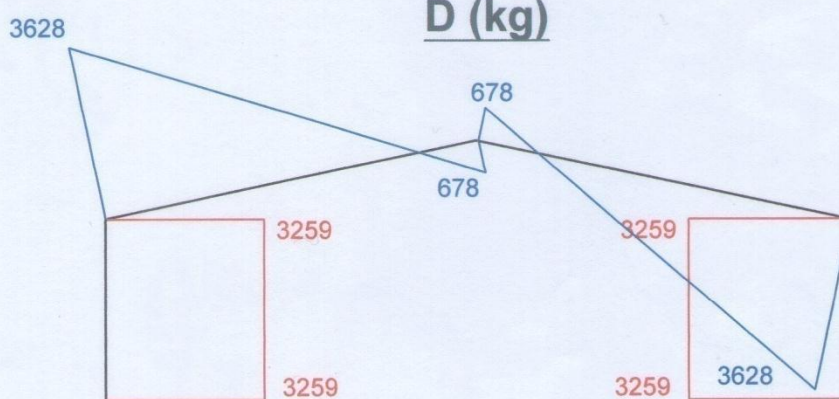
Tabel 2 - Perhitungan Momen Per Interval Bentang 2																	
x →	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	
-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	
-87	0	-42	-167	-375	-667	-1042	-1500	-2042	-2667	-3376	-4168	-5043	-6001	-7043	-8169	-9379	
0 x cos12 = -773	0	-773	-1545	-2318	-3090	-3863	-4636	-5408	-6181	-6953	-7726	-8499	-9271	-10044	-10816	-11588	
2 x cos12 = 4306	0	4306	8612	12918	17224	21529	25835	30141	34447	38753	43059	47365	51671	55976	60282	64588	
59 x sin12 = -678	0	-677,5	-1355	-2033	-2710	-3388	-4065	-4743	-5420	-6098	-6775	-7453	-8130	-8808	-9486	-10164	
6 x cos12 = -192			-134	-326	-517	-709	-900	-1092	-1284	-1475	-1667	-1858	-2050	-2241	-2433	-2625	
				-77	-268	-460	-651	-843	-1035	-1226	-1418	-1609	-1801	-1992	-2184	-2375	
					-19	-211	-402	-594	-785	-977	-1169	-1360	-1552	-1743	-1935	-2126	
							-153	-345	-536	-728	-920	-1111	-1303	-1494	-1686	-1877	
								-96	-287	-479	-671	-862	-1054	-1245	-1437	-1628	
									-38	-230	-421	-613	-805	-996	-1188	-1379	
											-172	-364	-556	-747	-939	-1130	
												-115	-307	-498	-690	-881	
													-57	-249	-441	-632	
															-192	-383	
																-574	
Jumlah	-13203	-10389	-7792	-5413	-3252	-1346	324	1775	3010	4007	4749	5274	5581	5671	5485	5013	

x →			0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	15,693	
M	-13203		-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	-13203	
q	-87		0	-42	-167	-375	-667	-1042	-1500	-2042	-2667	-3376	-4168	-5043	-6001	-7043	-8169	-9377	-10264	
P	-790	x cos12 = -773	0	-773	-1545	-2318	-3090	-3863	-4636	-5408	-6181	-6953	-7726	-8499	-9271	-10044	-10816	-11589	-12124	
V2	4402	x cos12 = 4306	0	4306	8612	12918	17224	21529	25835	30141	34447	38753	43059	47365	51671	55976	60282	64588	67572	
H2	-3259	x sin12 = -678	0	-677,5	-1355	-2033	-2710	-3388	-4065	-4743	-5420	-6098	-6775	-7453	-8130	-8808	-9486	-10163	-10633	
1,30	-196	x cos12 = -192			-134	-326	-517	-709	-900	-1092	-1284	-1475	-1667	-1858	-2050	-2241	-2433	-2625	-2757	
2,60						-77	-268	-460	-651	-843	-1035	-1226	-1418	-1609	-1801	-1992	-2184	-2376	-2508	
3,90							-19	-211	-402	-594	-785	-977	-1169	-1360	-1552	-1743	-1935	-2127	-2259	
5,20									-153	-345	-536	-728	-920	-1111	-1303	-1494	-1686	-1877	-2010	
6,50											-96	-287	-479	-671	-862	-1054	-1245	-1437	-1628	-1761
7,80												-38	-230	-421	-613	-805	-996	-1188	-1379	-1512
9,10														-172	-364	-556	-747	-939	-1130	-1263
10,40															-115	-307	-498	-690	-881	-1014
11,70																-57	-249	-441	-632	-765
13,00																			-192	-383
14,30																		-134	-267	
Jumlah			-13203	-10389	-7792	-5413	-3252	-1346	324	1775	3010	4007	4749	5274	5581	5671	5485	5082	4715	
																			Kr(%)	0

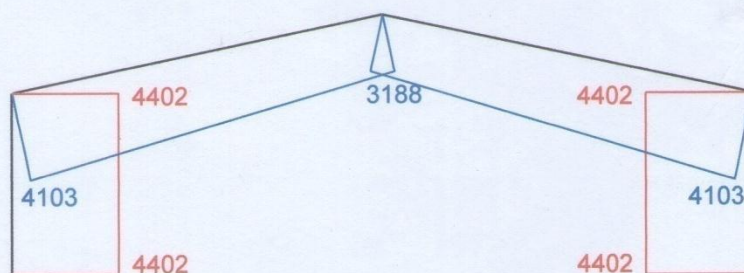
M (kgm)



D (kg)



N (kg)





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Job No

Sheet No

5

Rev

Part

Ref

By

Date 12-Mar-13

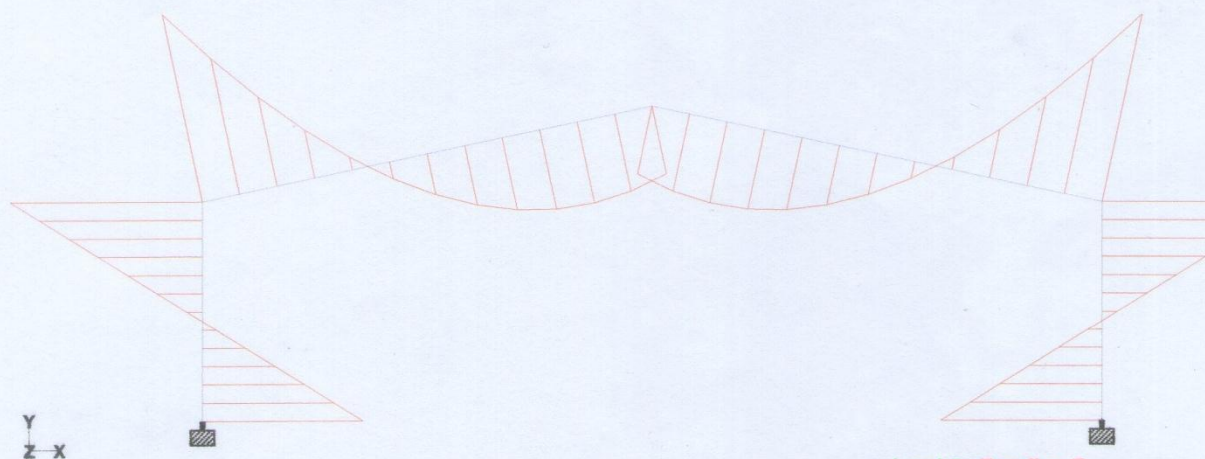
Chd

Job Title

Client

File Structure1.std

Date/Time 12-Mar-2013 13:24



Load 5 : Bending Z

Whole Structure Mz 2039.43kg-m:1m 5 COMBINATION LOAD CASE 5



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Job No

Sheet No

6

Rev

Part

Ref

By

Date 12-Mar-13

Chd

Job Title

Client

File Structure1.std

Date/Time 12-Mar-2013 13:24

Y
Z-X

Load 5 : Shear Y

Whole Structure Fy 407.886kg:1m 5 COMBINATION LOAD CASE 5



Software licensed to Toshiba

Job No

Sheet No

7

Rev

Part

Ref

By

Date 12-Mar-13

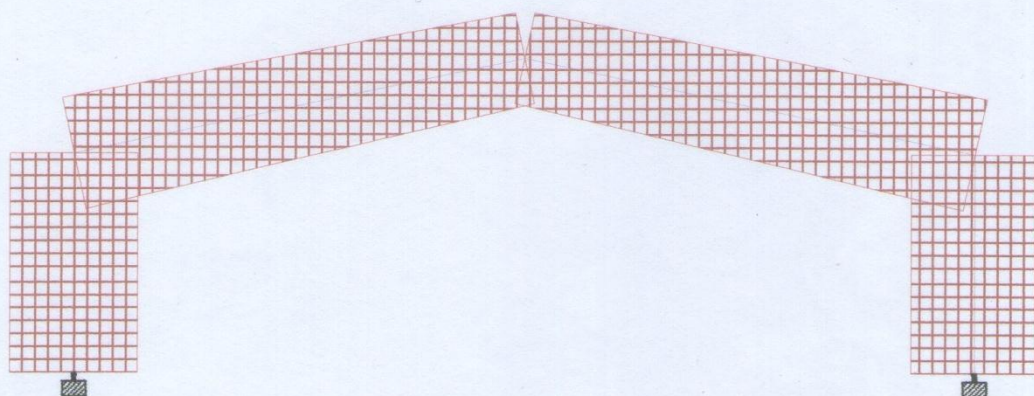
Chd

Client

File Structure1.std

Date/Time 12-Mar-2013 13:24

Y
Z-X



Load 5 : Axial Force

Whole Structure Fx 2039.43kg:1m 5 COMBINATION LOAD CASE 5

• **Kombinasi 3**

$$1.2D + 1.6(La \text{ atau } H) + (\gamma_L \cdot L \text{ atau } 0.8W)$$

$La < H \rightarrow$ dipakai H

Kombinasi pembebanannya menjadi:

$$1.2D + 1.6H + 0.8W$$

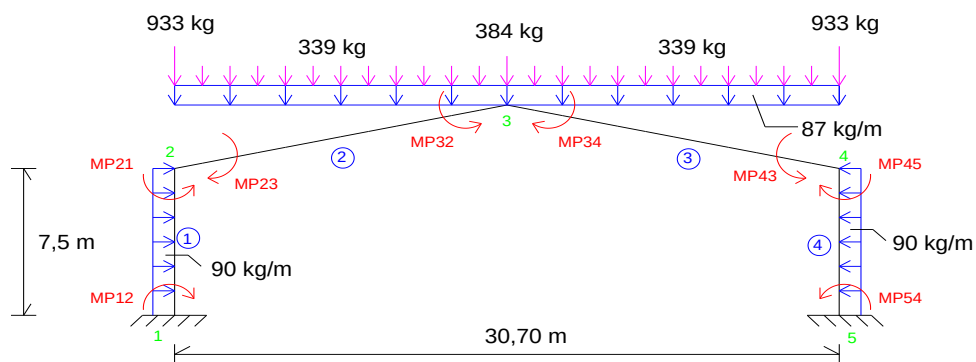
$$1,2 q_D = 1,2 \times 73 = 87 \text{ kg/m}$$

$$1,2 P_D: 1,2 \times 109 + 1,6 \times 130 = 339 \text{ kg}$$

$$1,2 \times 147 + 1,6 \times 130 = 384 \text{ kg}$$

$$1,2 \times 604 + 1,6 \times 130 = 933 \text{ kg}$$

$$0,8 W = 0,8 \times 113 = 90 \text{ kg/m}$$



	$\Sigma M3$		$\Sigma M2$	
Beban	Jarak	PxL	Jarak	PxL
87	15,35	10264	15,35	10264
192	0	0	15,35	2947
933	15,35	14319	0	0
339	14,08	4770,6	1,27	431
	12,81	4339,7	2,54	862
	11,54	3908,8	3,81	1293
	10,26	3477,9	5,09	1724
	8,99	3047	6,36	2154
	7,72	2616,2	7,63	2585
	6,45	2185,3	8,90	3016
	5,18	1754,4	10,17	3447
	3,91	1323,5	11,44	3878
	2,63	892,58	12,72	4309
	1,36	461,69	13,99	4740
Jumlah		53361	41649	
R2		3476	R3	2713

KONTROL				
87	x	15,35	=	1337
339	x	11	=	3727
384	x	0,5	=	192
933	x	1	=	933
Jumlah			6190	6190
OK				

$$MP12 = -MP21 = MP45 = -MP54$$

$$= \frac{1}{12} qL^2$$

$$= 421,88 \text{ kgm}$$

$$H1 = H2 = H4 = H5 = 338 \text{ kg}$$

- Momen Primer

$$MP_{23} = -MP_{32} = MP_{34} = -MP_{43}$$

$$= \frac{1}{12} qL^2 + \sum \frac{Pab^2}{L^2}$$

c	q	L ²	$\frac{1}{12} qL^2$
$\frac{1}{12}$	87	235,6	1710,6
P	a	b ²	$\frac{Pab^2}{L^2}$
933	0	236	0
339	1,27	198	362
339	2,54	164	600
339	3,81	133	730
339	5,09	105	771
339	6,36	81	739
339	7,63	60	654
339	8,90	42	532
339	10,17	27	392
339	11,44	15	251
339	12,72	7	127
339	13,99	2	37
384	15,35	0	0
MP (kgm)			6907

•Kombinasi 3 - Beban Ekuivalen {Fs}

$$\{Fs\} = \begin{Bmatrix} 338 \\ 0 \\ -422 \\ 338 \\ -3476 \\ -6485 \\ 0 \\ -5427 \\ 0 \\ -338 \\ -3476 \\ 6485 \\ -338 \\ 0 \\ 422 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix} \quad \begin{Bmatrix} F4 \\ F5 \\ F6 \\ F7 \\ F8 \\ F9 \\ F10 \\ F11 \\ F12 \\ F1 \\ F2 \\ F3 \\ F13 \\ F14 \\ F15 \end{Bmatrix} = \begin{Bmatrix} 338 \\ -3476 \\ -6485 \\ 0 \\ -5427 \\ 0 \\ -338 \\ -3476 \\ 6485 \\ 338 \\ 0 \\ -422 \\ -338 \\ 0 \\ 422 \end{Bmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{matrix}$$

i 3 - Per
 s} = [Ss]
 5
 3,21E
 4,46E
 -8,55E
 7,94E
 2,23E
 -1,75E
 3,21E
 1,57E
 -8,55E
 i 3 - Per
 s} = [Ss]
 5
 0
 -2243
 0
 0
 0
 0

i 3 - Per
 s} = [Ss]
 5
 3,21E
 4,46E
 -8,55E
 7,94E
 2,23E
 -1,75E
 3,21E
 1,57E
 -8,55E
 i 3 - Per
 s} = [Ss]
 5
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i 3 - Per
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 5
 3,21E
 4,46E
 -8,55E
 7,94E
 2,23E
 -1,75E
 3,21E
 1,57E
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 i 3 - Per
 s} = [Ss]
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i 3 - Per
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 3,21E
 4,46E
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 2,23E
 -1,75E
 3,21E
 1,57E
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 i 3 - Per
 s} = [Ss]
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i 3 - Per
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 3,21E
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 -1,75E
 3,21E
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i 3 - Per
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 5
 3,21E
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 -8,55E
 7,94E
 2,23E
 -1,75E
 3,21E
 1,57E
 -8,55E
 i 3 - Per
 s} = [Ss]
 5
 0
 -2243
 0
 0
 0
 0



•Kombinasi 3 - Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu batang)

Rumus: $\{Fm^A\}_i = \{Fm^B\}_i + [Sm]_i \times [RT]_i \times \{Ds\}_i$

dengan: $\{Fm^A\}_i$ = Gaya dalam batang

$\{Fm^B\}_i$ = Gaya akibat beban luar

$[Sm]_i$ = Matriks kekakuan batang (pada sumbu batang)

$[RT]_i$ = Matriks rotasi

$\{Ds\}_i$ = Perpindahan

$$\begin{aligned} \{Fm^A\}_1 &= \begin{Bmatrix} 0 \\ 338 \\ 422 \\ 0 \\ 338 \\ -422 \end{Bmatrix} + \begin{Bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{Bmatrix} \times \begin{Bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0 \\ 0 \\ 0 \\ -0,0260 \\ -0,0003 \\ -0,0022 \end{Bmatrix} = \begin{Bmatrix} 6190 \\ -4261 \\ -15459 \\ -6190 \\ 4936 \\ -19028 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix} \\ \{Fm^A\}_2 &= \begin{Bmatrix} 723 \\ 3400 \\ 6907 \\ 564 \\ 2654 \\ -6907 \end{Bmatrix} + \begin{Bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{Bmatrix} \times \begin{Bmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,21 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,21 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} -0,0260 \\ -0,0003 \\ -0,0022 \\ 0,0000 \\ -0,1251 \\ 0,0000 \end{Bmatrix} = \begin{Bmatrix} 6115 \\ 5028 \\ 19028 \\ -4828 \\ 1026 \\ 6517 \end{Bmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix} \\ \{Fm^A\}_3 &= \begin{Bmatrix} -564 \\ 2654 \\ 6907 \\ -723 \\ 3400 \\ -6907 \end{Bmatrix} + \begin{Bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{Bmatrix} \times \begin{Bmatrix} 0,978 & -0,21 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,21 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0000 \\ -0,1251 \\ 0,0000 \\ 0,0260 \\ -0,0003 \\ 0,0022 \end{Bmatrix} = \begin{Bmatrix} 4828 \\ 1026 \\ -6517 \\ -6115 \\ 5028 \\ -19028 \end{Bmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix} \\ \{Fm^A\}_4 &= \begin{Bmatrix} 0 \\ 338 \\ 422 \\ 0 \\ 338 \\ -422 \end{Bmatrix} + \begin{Bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{Bmatrix} \times \begin{Bmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0260 \\ -0,0003 \\ 0,0022 \\ 0 \\ 0 \\ 0 \end{Bmatrix} = \begin{Bmatrix} 6190 \\ 4936 \\ 19028 \\ -6190 \\ -4261 \\ 15459 \end{Bmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$



•Kombinasi 3 - Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu struktur)

Rumus: $\{F_s^A\}_i = [RT]^T_i \times \{F_m^A\}_i$

dengan: $\{F_s^A\}_i$ = Gaya dalam akhir batang

$[RT]^T_i$ = Matriks rotasi transpose

$\{F_m^A\}_i$ = Gaya dalam batang

$$\{F_s^A\}_1 = \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 6190 \\ -4261 \\ -15459 \\ -6190 \\ 4936 \\ -19028 \end{pmatrix} = \begin{pmatrix} 4261 \\ 6190 \\ -15459 \\ -4936 \\ -6190 \\ -19028 \end{pmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}$$

$$\{F_s^A\}_2 = \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 6115 \\ 5028 \\ 19028 \\ -4828 \\ 1026 \\ 6517 \end{pmatrix} = \begin{pmatrix} 4936 \\ 6190 \\ 19028 \\ -4936 \\ 0 \\ 6517 \end{pmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

$$\{F_s^A\}_3 = \begin{pmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4828 \\ 1026 \\ -6517 \\ -6115 \\ 5028 \\ -19028 \end{pmatrix} = \begin{pmatrix} 4936 \\ 0 \\ -6517 \\ -4936 \\ 6190 \\ -19028 \end{pmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\{F_s^A\}_4 = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 6190 \\ 4936 \\ 19028 \\ -6190 \\ -4261 \\ 15459 \end{pmatrix} = \begin{pmatrix} 4936 \\ -6190 \\ 19028 \\ -4261 \\ 6190 \\ 15459 \end{pmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$

Tabel 3 - Perhitungan Momen Per Interval Bentang 2																
$x \rightarrow$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028
-87	0	-42	-167	-375	-667	-1042	-1500	-2042	-2667	-3376	-4168	-5043	-6001	-7043	-8169	-9379
$x \cos 12^\circ = -912$	0	-912	-1825	-2737	-3650	-4562	-5475	-6387	-7300	-8212	-9125	-10037	-10950	-11862	-12775	-13687
$x \cos 12^\circ = 6054$	0	6054	12109	18163	24217	30272	36326	42380	48435	54489	60543	66597	72652	78706	84760	90814
$x \sin 12^\circ = -1026$	0	-1026	-2052	-3079	-4105	-5131	-6157	-7183	-8210	-9236	-10262	-11288	-12314	-13341	-14367	-15393
$x \cos 12^\circ = -331$			-232	-563	-895	-1226	-1558	-1889	-2221	-2552	-2884	-3215	-3547	-3878	-4209	-4539
				-133	-464	-795	-1127	-1458	-1790	-2121	-2453	-2784	-3116	-3447	-3779	-4110
					-33	-365	-696	-1028	-1359	-1690	-2022	-2353	-2685	-3016	-3348	-3679
							-265	-597	-928	-1260	-1591	-1922	-2254	-2585	-2917	-3248
								-166	-497	-829	-1160	-1492	-1823	-2154	-2486	-2817
									-66	-398	-729	-1061	-1392	-1724	-2055	-2386
										-298	-630	-961	-1293	-1624	-1955	-2286
											-199	-530	-862	-1193	-1524	-1855
												-99	-431	-762	-1093	-1424
														-331	-662	-993
															-331	-662
																-331
Jumlah	-19028	-14954	-11195	-7752	-4624	-1878	519	2602	4369	5787	6824	7545	7951	8042	7718	7028

Tabel 3 - Perhitungan Momen Per Interval Bentang 2																
$x \rightarrow$	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028	-19028
-87	0	-42	-167	-375	-667	-1042	-1500	-2042	-2667	-3376	-4168	-5043	-6001	-7043	-8169	-9380
$x \cos 12^\circ = -912$	0	-912	-1825	-2737	-3650	-4562	-5475	-6387	-7300	-8212	-9125	-10037	-10950	-11862	-12775	-13687
$x \cos 12^\circ = 6054$	0	6054	12109	18163	24217	30272	36326	42380	48435	54489	60543	66597	72652	78706	84760	90814
$x \sin 12^\circ = -1026$	0	-1026	-2052	-3079	-4105	-5131	-6157	-7183	-8210	-9236	-10262	-11288	-12314	-13341	-14367	-15393
$x \cos 12^\circ = -331$			-232	-563	-895	-1226	-1558	-1889	-2221	-2552	-2884	-3215	-3547	-3878	-4209	-4540
				-133	-464	-795	-1127	-1458	-1790	-2121	-2453	-2784	-3116	-3447	-3779	-4110
					-33	-365	-696	-1028	-1359	-1690	-2022	-2353	-2685	-3016	-3348	-3680
							-265	-597	-928	-1260	-1591	-1922	-2254	-2585	-2917	-3248
								-166	-497	-829	-1160	-1492	-1823	-2154	-2486	-2817
									-66	-398	-729	-1061	-1392	-1724	-2055	-2386
										-298	-630	-961	-1293	-1624	-1955	-2286
											-199	-530	-862	-1193	-1524	-1855
												-99	-431	-762	-1093	-1424
														-331	-662	-993
															-331	-662
																-331
Jumlah	-19028	-14954	-11195	-7752	-4624	-1878	519	2602	4369	5787	6824	7545	7951	8042	7718	7028

- Kombinasi 4**

$$1.2D + 1.3W + \gamma_L.L + 0.5(La \text{ atau } H)$$

$La < H \rightarrow$ dipakai H

Kombinasi pembebanannya menjadi:

$$1.2D + 1.3W + 0.5H$$

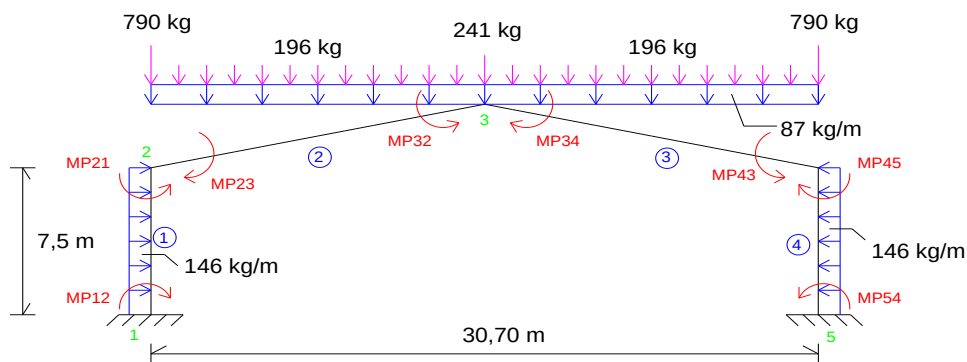
$$1,2 q_D = 1,2 \times 73 = 87 \text{ kg/m}$$

$$1,2 P_D: 1,2 \times 109 + 0,5 \times 130 = 196 \text{ kg}$$

$$1,2 \times 147 + 0,5 \times 130 = 241 \text{ kg}$$

$$1,2 \times 604 + 0,5 \times 130 = 790 \text{ kg}$$

$$1,3 W = 1,3 \times 113 = 146 \text{ kg/m}$$



	$\Sigma M3$		$\Sigma M2$	
Beban	Jarak	PxL	Jarak	PxL
87	15,35	10264	15,35	10264
120	0	0	15,35	1849
790	15,35	12124	0	0
196	14,08	2757,4	1,27	249
	12,81	2508,3	2,54	498
	11,54	2259,3	3,81	747
	10,26	2010,2	5,09	996
	8,99	1761,2	6,36	1245
	7,72	1512,1	7,63	1494
	6,45	1263,1	8,90	1743
	5,18	1014	10,17	1992
	3,91	764,97	11,44	2241
	2,63	515,91	12,72	2491
	1,36	266,86	13,99	2740
Jumlah		39021		28550
R2		2542	R3	1860

KONTROL				
87	x	15,35	=	1337
196	x	11	=	2154
241	x	0,5	=	120
790	x	1	=	790
Jumlah				4402
				4402
OK				

$$MP12 = -MP21 = MP45 = -MP54$$

$$= \frac{1}{12} qL^2$$

$$= 685,55 \text{ kgm}$$

$$H1 = H2 = H4 = H5 = 548 \text{ kg}$$

- Momen Primer

$$MP_{23} = -MP_{32} = MP_{34} = -MP_{43}$$

$$= \frac{1}{12} qL^2 + \sum \frac{Pab^2}{L^2}$$

c	q	L ²	$\frac{1}{12} qL^2$
$\frac{1}{12}$	87	235,6	1710,6
P	a	b ²	$\frac{Pab^2}{L^2}$
790	0	236	0
196	1,27	198	209
196	2,54	164	347
196	3,81	133	422
196	5,09	105	445
196	6,36	81	427
196	7,63	60	378
196	8,90	42	308
196	10,17	27	227
196	11,44	15	145
196	12,72	7	73
196	13,99	2	22
241	15,35	0	0
MP (kgm)			4714

•Kombinasi 4 - Beban Ekuivalen {Fs}

{Fs}	=	548	1	F4	=	548	4
		0	2	F5		-2542	5
		-686	3	F6		-4028	6
		548	4	F7		0	7
		-2542	5	F8		-3720	8
		-4028	6	F9		0	9
		0	7	F10		-548	10
		-3720	8	F11		-2542	11
		0	9	F12		4028	12
		-548	10	F1		548	1
		-2542	11	F2		0	2
		4028	12	F3		-686	3
		-548	13	F13		-548	13
		0	14	F14		0	14
		686	15	F15		686	15



repo
 i 4 - Per
 s} = [Ss]
 5
 3,21E
 4,46E
 -8,55E
 7,94E
 2,23E
 -1,75E
 3,21E
 1,57E
 -8,55E
 i 4 - Per
 s} = [Ss]
 5
 0
 -2243
 0
 0
 0
 0
 s
 AYA

repo
 i 4 - Per
 s} = [Ss]
 5
 3,21E
 4,46E
 -8,55E
 7,94E
 2,23E
 -1,75E
 3,21E
 1,57E
 -8,55E
 i 4 - Per
 s} = [Ss]
 5
 0
 -2243
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repo
 i 4 - Per
 s} = [Ss]
 5
 3,21E
 4,46E
 -8,55E
 7,94E
 2,23E
 -1,75E
 3,21E
 1,57E
 -8,55E
 i 4 - Per
 s} = [Ss]
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 i 4 - Per
 s} = [Ss]
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 3,21E
 4,46E
 -8,55E
 7,94E
 2,23E
 -1,75E
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 1,57E
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 i 4 - Per
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repo
 i 4 - Per
 s} = [Ss]
 5
 3,21E
 4,46E
 -8,55E
 7,94E
 2,23E
 -1,75E
 3,21E
 1,57E
 -8,55E
 i 4 - Per
 s} = [Ss]
 5
 0
 -2243
 0
 0
 0
 0
 s
 AYA



•Kombinasi 4 - Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu batang)

Rumus: $\{Fm^A\}_i = \{Fm^B\}_i + [Sm]_i \times [RT]_i \times \{Ds\}_i$

dengan: $\{Fm^A\}_i$ = Gaya dalam batang

$\{Fm^B\}_i$ = Gaya akibat beban luar

$[Sm]_i$ = Matriks kekakuan batang (pada sumbu batang)

$[RT]_i$ = Matriks rotasi

$\{Ds\}_i$ = Perpindahan

$$\{Fm^A\}_1 = \begin{Bmatrix} 0 \\ 548 \\ 686 \\ 0 \\ 548 \\ -686 \end{Bmatrix} + \begin{Bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{Bmatrix} \times \begin{Bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0 \\ 0 \\ 0 \\ -0,0171 \\ -0,0002 \\ -0,0014 \end{Bmatrix} = \begin{Bmatrix} 4402 \\ -2451 \\ -9702 \\ -4402 \\ 3548 \\ -12791 \end{Bmatrix}$$

$$\{Fm^A\}_2 = \begin{Bmatrix} 529 \\ 2487 \\ 4714 \\ 387 \\ 1819 \\ -4714 \end{Bmatrix} + \begin{Bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{Bmatrix} \times \begin{Bmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,21 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,21 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} -0,0171 \\ -0,0002 \\ -0,0014 \\ 0,0000 \\ -0,0826 \\ 0,0000 \end{Bmatrix} = \begin{Bmatrix} 4385 \\ 3568 \\ 12791 \\ -3470 \\ 738 \\ 4184 \end{Bmatrix}$$

$$\{Fm^A\}_3 = \begin{Bmatrix} -387 \\ 1819 \\ 4714 \\ -529 \\ 2487 \\ -4714 \end{Bmatrix} + \begin{Bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{Bmatrix} \times \begin{Bmatrix} 0,978 & -0,21 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,21 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0000 \\ -0,0826 \\ 0,0000 \\ 0,0171 \\ -0,0002 \\ 0,0014 \end{Bmatrix} = \begin{Bmatrix} 3470 \\ 738 \\ -4184 \\ -4385 \\ 3568 \\ -12791 \end{Bmatrix}$$

$$\{Fm^A\}_4 = \begin{Bmatrix} 0 \\ 548 \\ 686 \\ 0 \\ 548 \\ -686 \end{Bmatrix} + \begin{Bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{Bmatrix} \times \begin{Bmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0171 \\ -0,0002 \\ 0,0014 \\ 0 \\ 0 \\ 0 \end{Bmatrix} = \begin{Bmatrix} 4402 \\ 3548 \\ 12791 \\ -4402 \\ -2451 \\ 9702 \end{Bmatrix}$$



•Kombinasi 4 - Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu struktur)

Rumus: $\{F_s^A\}_i = [RT]^T_i \times \{F_m^A\}_i$

dengan: $\{F_s^A\}_i =$ Gaya dalam akhir batang

$[RT]^T_i =$ Matriks rotasi transpose

$\{F_m^A\}_i =$ Gaya dalam batang

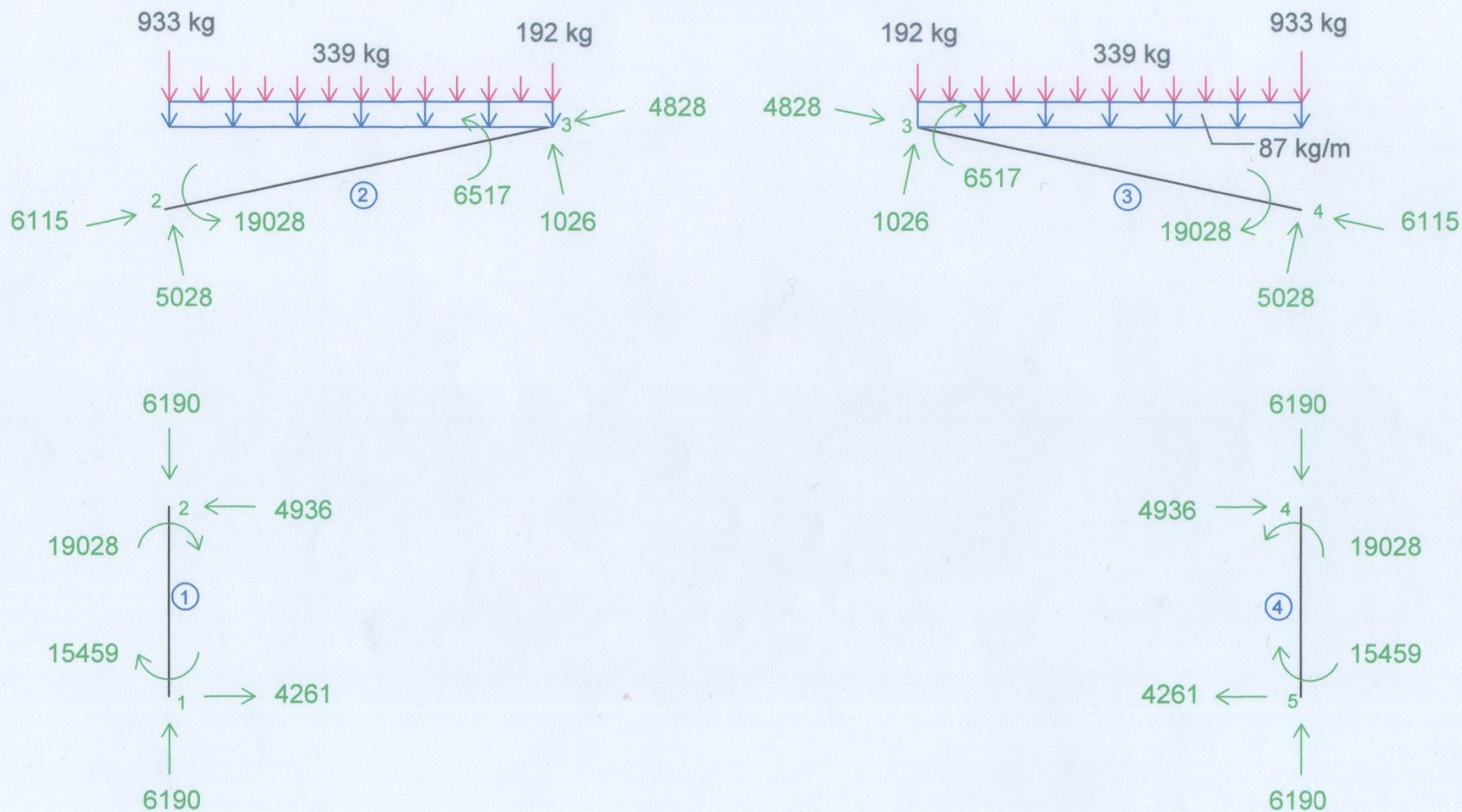
$$\{F_s^A\}_1 = \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4402 \\ -2451 \\ -9702 \\ -4402 \\ 3548 \\ -12791 \end{pmatrix} = \begin{pmatrix} 2451 \\ 4402 \\ -9702 \\ -3548 \\ -4402 \\ -12791 \end{pmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}$$

$$\{F_s^A\}_2 = \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4385 \\ 3568 \\ 12791 \\ -3470 \\ 738 \\ 4184 \end{pmatrix} = \begin{pmatrix} 3548 \\ 4402 \\ 12791 \\ -3548 \\ 0 \\ 4184 \end{pmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

$$\{F_s^A\}_3 = \begin{pmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 3470 \\ 738 \\ -4184 \\ -4385 \\ 3568 \\ -12791 \end{pmatrix} = \begin{pmatrix} 3548 \\ 0 \\ -4184 \\ -3548 \\ 4402 \\ -12791 \end{pmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\{F_s^A\}_4 = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4402 \\ 3548 \\ 12791 \\ -4402 \\ -2451 \\ 9702 \end{pmatrix} = \begin{pmatrix} 3548 \\ -4402 \\ 12791 \\ -2451 \\ 4402 \\ 9702 \end{pmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$

FBD KOMBINASI 3



Tabel 4 - Perhitungan Momen Per Interval Bentang 2																	
x →	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791
-87	0	-42	-167	-375	-667	-1042	-1500	-2042	-2667	-3376	-4168	-5043	-6001	-7043	-8169	-9389	-10699
90 x cos12 = -773	0	-773	-1545	-2318	-3090	-3863	-4636	-5408	-6181	-6953	-7726	-8499	-9271	-10044	-10816	-11588	-12359
02 x cos12 = 4306	0	4306	8612	12918	17224	21529	25835	30141	34447	38753	43059	47365	51671	55976	60282	64588	68894
48 x sin12 = -738	0	-737,6	-1475	-2213	-2950	-3688	-4425	-5163	-5901	-6638	-7376	-8113	-8851	-9588	-10326	-11064	-11801
96 x cos12 = -192			-134	-326	-517	-709	-900	-1092	-1284	-1475	-1667	-1858	-2050	-2241	-2433	-2625	-2816
				-77	-268	-460	-651	-843	-1035	-1226	-1418	-1609	-1801	-1992	-2184	-2375	-2566
					-19	-211	-402	-594	-785	-977	-1169	-1360	-1552	-1743	-1935	-2126	-2317
							-153	-345	-536	-728	-920	-1111	-1303	-1494	-1686	-1877	-2068
								-96	-287	-479	-671	-862	-1054	-1245	-1437	-1628	-1819
									-38	-230	-421	-613	-805	-996	-1188	-1379	-1570
											-172	-364	-556	-747	-939	-1130	-1321
												-115	-307	-498	-690	-881	-1072
													-57	-249	-441	-632	-823
															-192	-384	-576
Jumlah	-12791	-10037	-7501	-5181	-3080	-1234	375	1767	2941	3879	4561	5026	5273	5302	5057	4499	3749

x →			0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	15,693	
M	-12791		-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	-12791	
q	-87		0	-42	-167	-375	-667	-1042	-1500	-2042	-2667	-3376	-4168	-5043	-6001	-7043	-8169	-9377	-10264	
P	-790	x cos12 = -773	0	-773	-1545	-2318	-3090	-3863	-4636	-5408	-6181	-6953	-7726	-8499	-9271	-10044	-10816	-11589	-12124	
V2	4402	x cos12 = 4306	0	4306	8612	12918	17224	21529	25835	30141	34447	38753	43059	47365	51671	55976	60282	64588	67572	
H2	-3548	x sin12 = -738	0	-737,6	-1475	-2213	-2950	-3688	-4425	-5163	-5901	-6638	-7376	-8113	-8851	-9588	-10326	-11064	-11575	
1,30	-196	x cos12 = -192			-134	-326	-517	-709	-900	-1092	-1284	-1475	-1667	-1858	-2050	-2241	-2433	-2625	-2757	
2,60						-77	-268	-460	-651	-843	-1035	-1226	-1418	-1609	-1801	-1992	-2184	-2376	-2508	
3,90							-19	-211	-402	-594	-785	-977	-1169	-1360	-1552	-1743	-1935	-2127	-2259	
5,20									-153	-345	-536	-728	-920	-1111	-1303	-1494	-1686	-1877	-2010	
6,50											-96	-287	-479	-671	-862	-1054	-1245	-1437	-1628	-1761
7,80												-38	-230	-421	-613	-805	-996	-1188	-1379	-1512
9,10														-172	-364	-556	-747	-939	-1130	-1263
10,40															-115	-307	-498	-690	-881	-1014
11,70																-57	-249	-441	-632	-765
13,00																		-192	-383	-516
14,30																		-134	-267	
Jumlah			-12791	-10037	-7501	-5181	-3080	-1234	375	1767	2941	3879	4561	5026	5273	5302	5057	4594	4184	
																			Kr(%)	0

• **Beban Ekvivalen Mntu {Fs}**

$$\{F_s\} = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -3476 \\ -6907 \\ 0 \\ -5427 \\ 0 \\ 0 \\ -3476 \\ 6907 \\ 0 \\ 0 \\ 0 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$

$$\begin{matrix} F4 \\ F5 \\ F6 \\ F7 \\ F8 \\ F9 \\ F10 \\ F11 \\ F12 \end{matrix} = \begin{Bmatrix} 0 \\ -3476 \\ -6907 \\ 0 \\ -5427 \\ 0 \\ 0 \\ -3476 \\ 6907 \end{Bmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\begin{matrix} F1 \\ F2 \\ F3 \\ F13 \\ F14 \\ F15 \end{matrix} = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{matrix}$$

• **Beban Ekvivalen Mltu {Fs}**

$$\{F_s\} = \begin{Bmatrix} 338 \\ 0 \\ -422 \\ 338 \\ 0 \\ 422 \\ 0 \\ 0 \\ 0 \\ -338 \\ 0 \\ -422 \\ -338 \\ 0 \\ 422 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$

$$\begin{matrix} F4 \\ F5 \\ F6 \\ F7 \\ F8 \\ F9 \\ F10 \\ F11 \\ F12 \end{matrix} = \begin{Bmatrix} 338 \\ 0 \\ 422 \\ 0 \\ 0 \\ 0 \\ -338 \\ 0 \\ -422 \end{Bmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\begin{matrix} F1 \\ F2 \\ F3 \\ F13 \\ F14 \\ F15 \end{matrix} = \begin{Bmatrix} 338 \\ 0 \\ -422 \\ -338 \\ 0 \\ 422 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{matrix}$$

BAB 6

Perhitungan Perpindahan – Beban Gravitasi

$\{Ds\} = [Ss]^{-1} \cdot \{Fs\}$

5	6	7	8	9	10	11	12
3,21E-09	-1,21E-06	8,28E-06	4,91E-06	6,09E-07	7,20E-06	-3,21E-09	-1,23E-06
4,46E-08	-8,55E-10	7,94E-09	2,23E-08	-1,75E-09	3,21E-09	1,57E-12	-8,55E-10
-8,55E-10	4,60E-07	-1,22E-06	7,61E-08	-1,62E-07	-1,23E-06	8,55E-10	1,90E-07
7,94E-09	-1,22E-06	8,33E-06	1,14E-20	6,08E-07	8,28E-06	-7,94E-09	-1,22E-06
2,23E-08	7,61E-08	7,53E-21	2,35E-05	9,41E-22	-4,91E-06	2,23E-08	-7,61E-08
-1,75E-09	-1,62E-07	6,08E-07	6,38E-23	4,95E-07	6,09E-07	1,75E-09	-1,62E-07
3,21E-09	-1,23E-06	8,28E-06	-4,91E-06	6,09E-07	9,36E-06	-3,21E-09	-1,21E-06
1,57E-12	8,55E-10	-7,94E-09	2,23E-08	1,75E-09	-3,21E-09	4,46E-08	8,55E-10
-8,55E-10	1,90E-07	-1,22E-06	-7,61E-08	-1,62E-07	-1,21E-06	8,55E-10	4,60E-07

$\begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix} \times \begin{Bmatrix} 0 \\ -3476 \\ -6907 \\ 0 \\ -5427 \\ 0 \\ 0 \\ 0 \\ -3476 \\ 6907 \end{Bmatrix} = \begin{Bmatrix} -0,0268 \\ -0,0003 \\ -0,0023 \\ 0,0000 \\ -0,1285 \\ 0,0000 \\ 0,0268 \\ -0,0003 \\ 0,0023 \end{Bmatrix}$

Perhitungan Reaksi Tumpuan – Beban Gravitasi

$\{Rs\} = [Ss] \cdot \{Ds\}$

5	6	7	8	9	10	11	12
0	-505600	0	0	0	0	0	0
-22432000	0	0	0	0	0	0	0
0	1264000	0	0	0	0	0	0
0	0	0	0	0	-134827	0	-505600
0	0	0	0	0	0	-22432000	0
0	0	0	0	0	505600	0	1264000

$\begin{matrix} 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{matrix} \times \begin{Bmatrix} -0,0268 \\ -0,0003 \\ -0,0023 \\ 0,0000 \\ -0,1285 \\ 0,0000 \end{Bmatrix} = \begin{Bmatrix} 4750 \\ 6190 \\ -16400 \\ -4750 \\ 6190 \\ 16400 \end{Bmatrix}$

BAB 6

Perhitungan Perpindahan – Beban Gravitasi

$\{Ds\} = [Ss]^{-1} \cdot \{Fs\}$

5	6	7	8	9	10	11	12
3,21E-09	-1,21E-06	8,28E-06	4,91E-06	6,09E-07	7,20E-06	-3,21E-09	-1,23E-06
4,46E-08	-8,55E-10	7,94E-09	2,23E-08	-1,75E-09	3,21E-09	1,57E-12	-8,55E-10
-8,55E-10	4,60E-07	-1,22E-06	7,61E-08	-1,62E-07	-1,23E-06	8,55E-10	1,90E-07
7,94E-09	-1,22E-06	8,33E-06	1,14E-20	6,08E-07	8,28E-06	-7,94E-09	-1,22E-06
2,23E-08	7,61E-08	7,53E-21	2,35E-05	9,41E-22	-4,91E-06	2,23E-08	-7,61E-08
-1,75E-09	-1,62E-07	6,08E-07	6,38E-23	4,95E-07	6,09E-07	1,75E-09	-1,62E-07
3,21E-09	-1,23E-06	8,28E-06	-4,91E-06	6,09E-07	9,36E-06	-3,21E-09	-1,21E-06
1,57E-12	8,55E-10	-7,94E-09	2,23E-08	1,75E-09	-3,21E-09	4,46E-08	8,55E-10
-8,55E-10	1,90E-07	-1,22E-06	-7,61E-08	-1,62E-07	-1,21E-06	8,55E-10	4,60E-07

$\begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix} \times \begin{Bmatrix} 0 \\ -3476 \\ -6907 \\ 0 \\ -5427 \\ 0 \\ 0 \\ 0 \\ -3476 \\ 6907 \end{Bmatrix} = \begin{Bmatrix} -0,0268 \\ -0,0003 \\ -0,0023 \\ 0,0000 \\ -0,1285 \\ 0,0000 \\ 0,0268 \\ -0,0003 \\ 0,0023 \end{Bmatrix}$

Perhitungan Reaksi Tumpuan – Beban Gravitasi

$\{Rs\} = [Ss] \cdot \{Ds\}$

5	6	7	8	9	10	11	12
0	-505600	0	0	0	0	0	0
-22432000	0	0	0	0	0	0	0
0	1264000	0	0	0	0	0	0
0	0	0	0	0	-134827	0	-505600
0	0	0	0	0	0	-22432000	0
0	0	0	0	0	505600	0	1264000

$\begin{matrix} 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{matrix} \times \begin{Bmatrix} -0,0268 \\ -0,0003 \\ -0,0023 \\ 0,0000 \\ -0,1285 \\ 0,0000 \end{Bmatrix} = \begin{Bmatrix} 4750 \\ 6190 \\ -16400 \\ -4750 \\ 6190 \\ 16400 \end{Bmatrix}$

Perhitungan Perpindahan – Beban Gravitasi

$$\{Ds\} = [Ss]^{-1} \cdot \{Fs\}$$

5	6	7	8	9	10	11	12
3,21E-09	-1,21E-06	8,28E-06	4,91E-06	6,09E-07	7,20E-06	-3,21E-09	-1,23E-06
4,46E-08	-8,55E-10	7,94E-09	2,23E-08	-1,75E-09	3,21E-09	1,57E-12	-8,55E-10
-8,55E-10	4,60E-07	-1,22E-06	7,61E-08	-1,62E-07	-1,23E-06	8,55E-10	1,90E-07
7,94E-09	-1,22E-06	8,33E-06	1,14E-20	6,08E-07	8,28E-06	-7,94E-09	-1,22E-06
2,23E-08	7,61E-08	7,53E-21	2,35E-05	9,41E-22	-4,91E-06	2,23E-08	-7,61E-08
-1,75E-09	-1,62E-07	6,08E-07	6,38E-23	4,95E-07	6,09E-07	1,75E-09	-1,62E-07
3,21E-09	-1,23E-06	8,28E-06	-4,91E-06	6,09E-07	9,36E-06	-3,21E-09	-1,21E-06
1,57E-12	8,55E-10	-7,94E-09	2,23E-08	1,75E-09	-3,21E-09	4,46E-08	8,55E-10
-8,55E-10	1,90E-07	-1,22E-06	-7,61E-08	-1,62E-07	-1,21E-06	8,55E-10	4,60E-07

Matrix multiplication result:

$$\begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix} \times \begin{Bmatrix} 0 \\ -3476 \\ -6907 \\ 0 \\ -5427 \\ 0 \\ 0 \\ -3476 \\ 6907 \end{Bmatrix} = \begin{Bmatrix} -0,0268 \\ -0,0003 \\ -0,0023 \\ 0,0000 \\ -0,1285 \\ 0,0000 \\ 0,0268 \\ -0,0003 \\ 0,0023 \end{Bmatrix}$$

Perhitungan Reaksi Tumpuan – Beban Gravitasi

$$\{Rs\} = [Ss] \cdot \{Ds\}$$

5	6	7	8	9	10	11	12
0	-505600	0	0	0	0	0	0
-22432000	0	0	0	0	0	0	0
0	1264000	0	0	0	0	0	0
0	0	0	0	0	-134827	0	-505600
0	0	0	0	0	0	-22432000	0
0	0	0	0	0	505600	0	1264000

Matrix multiplication result:

$$\begin{matrix} 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{matrix} \times \begin{Bmatrix} -0,0268 \\ -0,0003 \\ -0,0023 \\ 0,0000 \\ -0,1285 \\ 0,0000 \\ 0,0268 \\ -0,0003 \\ 0,0023 \end{Bmatrix} = \begin{Bmatrix} 475 \\ 619 \\ -164 \\ -47 \\ 619 \\ 164 \end{Bmatrix}$$

[illegible]

[illegible]

Bahan

Perhitungan Perpindahan – Beban Gravitasi

$\{Ds\} = [Ss]^{-1} \cdot \{Fs\}$

5	6	7	8	9	10	11	12
3,21E-09	-1,21E-06	8,28E-06	4,91E-06	6,09E-07	7,20E-06	-3,21E-09	-1,23E-06
4,46E-08	-8,55E-10	7,94E-09	2,23E-08	-1,75E-09	3,21E-09	1,57E-12	-8,55E-10
-8,55E-10	4,60E-07	-1,22E-06	7,61E-08	-1,62E-07	-1,23E-06	8,55E-10	1,90E-07
7,94E-09	-1,22E-06	8,33E-06	1,14E-20	6,08E-07	8,28E-06	-7,94E-09	-1,22E-06
2,23E-08	7,61E-08	7,53E-21	2,35E-05	9,41E-22	-4,91E-06	2,23E-08	-7,61E-08
-1,75E-09	-1,62E-07	6,08E-07	6,38E-23	4,95E-07	6,09E-07	1,75E-09	-1,62E-07
3,21E-09	-1,23E-06	8,28E-06	-4,91E-06	6,09E-07	9,36E-06	-3,21E-09	-1,21E-06
1,57E-12	8,55E-10	-7,94E-09	2,23E-08	1,75E-09	-3,21E-09	4,46E-08	8,55E-10
-8,55E-10	1,90E-07	-1,22E-06	-7,61E-08	-1,62E-07	-1,21E-06	8,55E-10	4,60E-07

4 x { } = { }

5 -3476 -0,00

6 -6907 -0,00

7 0 0,00

8 -5427 -0,12

9 0 0,00

10 0 0,02

11 -3476 -0,00

12 6907 0,00

Perhitungan Reaksi Tumpuan – Beban Gravitasi

$\{Rs\} = [Ss] \cdot \{Ds\}$

5	6	7	8	9	10	11	12
0	-505600	0	0	0	0	0	0
-22432000	0	0	0	0	0	0	0
0	1264000	0	0	0	0	0	0
0	0	0	0	0	-134827	0	-505600
0	0	0	0	0	0	-22432000	0
0	0	0	0	0	505600	0	1264000

1 x { } = { }

2 -0,0268 475

3 -0,0003 619

4 -0,0023 -164

5 0,0000 -47

6 -0,1285 619

7 0,0000 164

8 0,0268

9 -0,0003

10 0,0023

• **Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu batang) – Beban Gravitasi**

Rumus: $\{F_m^A\}_i = \{F_m^B\}_i + [S_m]_i \times [RT]_i \times \{D_s\}_i$

dengan: $\{F_m^A\}_i$ = Gaya dalam batang
 $\{F_m^B\}_i$ = Gaya akibat beban luar
 $[S_m]_i$ = Matriks kekakuan batang (pada sumbu batang)
 $[RT]_i$ = Matriks rotasi
 $\{D_s\}_i$ = Perpindahan

$$\begin{aligned} \{F_m^A\}_1 &= \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} + \begin{bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{bmatrix} \times \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{Bmatrix} 0 \\ 0 \\ 0 \\ -0,0268 \\ -0,0003 \\ -0,0023 \end{Bmatrix} = \begin{Bmatrix} 6190 \\ -4758 \\ -16404 \\ -6190 \\ 4758 \\ -19281 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix} \\ \{F_m^A\}_2 &= \begin{Bmatrix} 723 \\ 3400 \\ 6907 \\ 564 \\ 2654 \\ -6907 \end{Bmatrix} + \begin{bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{bmatrix} \times \begin{bmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,21 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,21 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{Bmatrix} -0,0268 \\ -0,0003 \\ -0,0023 \\ 0,0000 \\ -0,1285 \\ 0,0000 \end{Bmatrix} = \begin{Bmatrix} 5941 \\ 5065 \\ 19281 \\ -4654 \\ 989 \\ 6843 \end{Bmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix} \end{aligned}$$

$$\{Fm^A\}_3 = \begin{Bmatrix} -564 \\ 2654 \\ 6907 \\ -723 \\ 3400 \\ -6907 \end{Bmatrix} + \begin{Bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{Bmatrix} \times \begin{Bmatrix} 0,978 & -0,21 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,21 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0000 \\ -0,1285 \\ 0,0000 \\ 0,0268 \\ -0,0003 \\ 0,0023 \end{Bmatrix} = \begin{Bmatrix} 4654 \\ 989 \\ -6843 \\ -5941 \\ 5065 \\ -19281 \end{Bmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\{Fm^A\}_4 = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} + \begin{Bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{Bmatrix} \times \begin{Bmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{Bmatrix} \times \begin{Bmatrix} 0,0268 \\ -0,0003 \\ 0,0023 \\ 0 \\ 0 \\ 0 \end{Bmatrix} = \begin{Bmatrix} 6190 \\ 4758 \\ 19281 \\ -6190 \\ -4758 \\ 16404 \end{Bmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$



- **Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu struktur) – Beban Gravitasi**

Rumus: $\{F_s^A\}_i = [RT]^T_i \times \{F_m^A\}_i$

dengan: $\{F_s^A\}_i$ = Gaya dalam akhir batang

$[RT]^T_i$ = Matriks rotasi transpose

$\{F_m^A\}_i$ = Gaya dalam batang

$$\{F_s^A\}_1 = \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 6190 \\ -4758 \\ -16404 \\ -6190 \\ 4758 \\ -19281 \end{pmatrix} = \begin{pmatrix} 4758 \\ 6190 \\ -16404 \\ -4758 \\ -6190 \\ -19281 \end{pmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}$$

$$\{F_s^A\}_2 = \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 5941 \\ 5065 \\ 19281 \\ -4654 \\ 989 \\ 6843 \end{pmatrix} = \begin{pmatrix} 4758 \\ 6190 \\ 19281 \\ -4758 \\ 0 \\ 6843 \end{pmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

$$\{F_s^A\}_3 = \begin{pmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 4654 \\ 989 \\ -6843 \\ -5941 \\ 5065 \\ -19281 \end{pmatrix} = \begin{pmatrix} 4758 \\ 0 \\ -6843 \\ -4758 \\ 6190 \\ -19281 \end{pmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\{F_s^A\}_4 = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 6190 \\ 4758 \\ 19281 \\ -6190 \\ -4758 \\ 16404 \end{pmatrix} = \begin{pmatrix} 4758 \\ -6190 \\ 19281 \\ -4758 \\ 6190 \\ 16404 \end{pmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$

Penghitungan Perpindahan – Beban Horizontal

$$\{Ds\} = [Ss]^{-1} \cdot \{Fs\}$$

5	6	7	8	9	10	11	12
3,21E-09	-1,21E-06	8,28E-06	4,91E-06	6,09E-07	7,20E-06	-3,21E-09	-1,23E-06
4,46E-08	-8,55E-10	7,94E-09	2,23E-08	-1,75E-09	3,21E-09	1,57E-12	-8,55E-10
-8,55E-10	4,60E-07	-1,22E-06	7,61E-08	-1,62E-07	-1,23E-06	8,55E-10	1,90E-07
7,94E-09	-1,22E-06	8,33E-06	1,14E-20	6,08E-07	8,28E-06	-7,94E-09	-1,22E-06
2,23E-08	7,61E-08	7,53E-21	2,35E-05	9,41E-22	-4,91E-06	2,23E-08	-7,61E-08
-1,75E-09	-1,62E-07	6,08E-07	6,38E-23	4,95E-07	6,09E-07	1,75E-09	-1,62E-07
3,21E-09	-1,23E-06	8,28E-06	-4,91E-06	6,09E-07	9,36E-06	-3,21E-09	-1,21E-06
1,57E-12	8,55E-10	-7,94E-09	2,23E-08	1,75E-09	-3,21E-09	4,46E-08	8,55E-10
-8,55E-10	1,90E-07	-1,22E-06	-7,61E-08	-1,62E-07	-1,21E-06	8,55E-10	4,60E-07

x {Fs} = {Ds}

4	5	6	7	8	9	10	11	12
338	0	422	0	0	0	-338	0	-422

= {Ds}

{Ds} = {Ds}

Penghitungan Reaksi Tumpuan – Beban Horizontal

$$\{Rs\} = [Ss] \cdot \{Ds\}$$

5	6	7	8	9	10	11	12
0	-505600	0	0	0	0	0	0
-22432000	0	0	0	0	0	0	0
0	1264000	0	0	0	0	0	0
0	0	0	0	0	-134827	0	-505600
0	0	0	0	0	0	-22432000	0
0	0	0	0	0	505600	0	1264000

x {Ds} = {Rs}

1	2	3	13	14	15
0,0007	0,0000	0,0001	0,0000	0,0034	0,0000
-0,0007	0,0000	-0,0001			

= {Rs}

Beban Pergerakan – Beban Horizontal

$$\{Ds\} = [Ss]^{-1} \cdot \{Fs\}$$

5	6	7	8	9	10	11	12
3,21E-09	-1,21E-06	8,28E-06	4,91E-06	6,09E-07	7,20E-06	-3,21E-09	-1,23E-06
4,46E-08	-8,55E-10	7,94E-09	2,23E-08	-1,75E-09	3,21E-09	1,57E-12	-8,55E-10
-8,55E-10	4,60E-07	-1,22E-06	7,61E-08	-1,62E-07	-1,23E-06	8,55E-10	1,90E-07
7,94E-09	-1,22E-06	8,33E-06	1,14E-20	6,08E-07	8,28E-06	-7,94E-09	-1,22E-06
2,23E-08	7,61E-08	7,53E-21	2,35E-05	9,41E-22	-4,91E-06	2,23E-08	-7,61E-08
-1,75E-09	-1,62E-07	6,08E-07	6,38E-23	4,95E-07	6,09E-07	1,75E-09	-1,62E-07
3,21E-09	-1,23E-06	8,28E-06	-4,91E-06	6,09E-07	9,36E-06	-3,21E-09	-1,21E-06
1,57E-12	8,55E-10	-7,94E-09	2,23E-08	1,75E-09	-3,21E-09	4,46E-08	8,55E-10
-8,55E-10	1,90E-07	-1,22E-06	-7,61E-08	-1,62E-07	-1,21E-06	8,55E-10	4,60E-07

x

4	5	6	7	8	9	10	11	12
338	0	422	0	0	0	-338	0	-422

=

4	5	6	7	8	9	10	11	12
0,00	0,00	0,00	0,00	0,00	0,00	-0,00	0,00	-0,00

Beban Reaksi Tumpuan – Beban Horizontal

$$\{Fs\} = [Ss] \cdot \{Ds\}$$

5	6	7	8	9	10	11	12
0	-505600	0	0	0	0	0	0
-22432000	0	0	0	0	0	0	0
0	1264000	0	0	0	0	0	0
0	0	0	0	0	-134827	0	-505600
0	0	0	0	0	0	-22432000	0
0	0	0	0	0	505600	0	1264000

x

1	2	3	13	14	15
0,0007	0,0000	0,0001	0,0000	0,0034	0,0000
-0,0007	0,0000	-0,0001			

=

1	2	3	13	14	15
-16	0	52	16	0	-52

Bahan Perencanaan Struktur

Perhitungan Perpindahan – Beban Horizontal

$\{Ds\} = [Ss]^{-1} \cdot \{Fs\}$

5	6	7	8	9	10	11	12
3,21E-09	-1,21E-06	8,28E-06	4,91E-06	6,09E-07	7,20E-06	-3,21E-09	-1,23E-06
4,46E-08	-8,55E-10	7,94E-09	2,23E-08	-1,75E-09	3,21E-09	1,57E-12	-8,55E-10
-8,55E-10	4,60E-07	-1,22E-06	7,61E-08	-1,62E-07	-1,23E-06	8,55E-10	1,90E-07
7,94E-09	-1,22E-06	8,33E-06	1,14E-20	6,08E-07	8,28E-06	-7,94E-09	-1,22E-06
2,23E-08	7,61E-08	7,53E-21	2,35E-05	9,41E-22	-4,91E-06	2,23E-08	-7,61E-08
-1,75E-09	-1,62E-07	6,08E-07	6,38E-23	4,95E-07	6,09E-07	1,75E-09	-1,62E-07
3,21E-09	-1,23E-06	8,28E-06	-4,91E-06	6,09E-07	9,36E-06	-3,21E-09	-1,21E-06
1,57E-12	8,55E-10	-7,94E-09	2,23E-08	1,75E-09	-3,21E-09	4,46E-08	8,55E-10
-8,55E-10	1,90E-07	-1,22E-06	-7,61E-08	-1,62E-07	-1,21E-06	8,55E-10	4,60E-07

$\begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix} \times \begin{Bmatrix} 338 \\ 0 \\ 422 \\ 0 \\ 0 \\ 0 \\ -338 \\ 0 \\ -422 \end{Bmatrix} = \begin{Bmatrix} 0,00 \\ 0,00 \\ 0,00 \\ 0,00 \\ 0,00 \\ 0,00 \\ -0,00 \\ 0,00 \\ -0,00 \end{Bmatrix}$

Perhitungan Reaksi Tumpuan – Beban Horizontal

$\{Rs\} = [Ss] \cdot \{Ds\}$

5	6	7	8	9	10	11	12
0	-505600	0	0	0	0	0	0
-22432000	0	0	0	0	0	0	0
0	1264000	0	0	0	0	0	0
0	0	0	0	0	-134827	0	-505600
0	0	0	0	0	0	-22432000	0
0	0	0	0	0	505600	0	1264000

$\begin{matrix} 1 \\ 2 \\ 3 \\ 13 \\ 14 \\ 15 \end{matrix} \times \begin{Bmatrix} 0,0007 \\ 0,0000 \\ 0,0001 \\ 0,0000 \\ 0,0034 \\ 0,0000 \\ -0,0007 \\ 0,0000 \\ -0,0001 \end{Bmatrix} = \begin{Bmatrix} -16 \\ 0 \\ 52 \\ 16 \\ 0 \\ -52 \end{Bmatrix}$

[illegible]

[illegible]

[illegible]

- Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu batang) – Beban Horisontal

Rumus: $\{F_m^A\}_i = \{F_m^B\}_i + [S_m]_i \times [RT]_i \times \{D_s\}_i$

dengan: $\{F_m^A\}_i$ = Gaya dalam batang

$\{F_m^B\}_i$ = Gaya akibat beban luar

$[S_m]_i$ = Matriks kekakuan batang (pada sumbu batang)

$[RT]_i$ = Matriks rotasi

$\{D_s\}_i$ = Perpindahan

$$\{F_m^A\}_1 = \begin{Bmatrix} 0 \\ 338 \\ 422 \\ 0 \\ 338 \\ -422 \end{Bmatrix} + \begin{bmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{bmatrix} \times \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0,0007 \\ 0,0000 \\ 0,0001 \end{Bmatrix} = \begin{Bmatrix} 0 \\ 497 \\ 945 \\ 0 \\ 178 \\ 254 \end{Bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}$$

$$\{F_m^A\}_2 = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} + \begin{bmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{bmatrix} \times \begin{bmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,21 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,21 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{Bmatrix} 0,0007 \\ 0,0000 \\ 0,0001 \\ 0,0000 \\ 0,0034 \\ 0,0000 \end{Bmatrix} = \begin{Bmatrix} 174 \\ -37 \\ -254 \\ -174 \\ 37 \\ -326 \end{Bmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

$$\{Fm^A\}_3 = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{Bmatrix} + \begin{pmatrix} 10720753 & 0 & 0 & -10720753 & 0 & 0 \\ 0 & 14718 & 115484 & 0 & -14718 & 115484 \\ 0 & 115484 & 1208188 & 0 & -115484 & 604094 \\ -10720753 & 0 & 0 & 10720753 & 0 & 0 \\ 0 & -14718 & -115484 & 0 & 14718 & -115484 \\ 0 & 115484 & 604094 & 0 & -115484 & 1208188 \end{pmatrix} \times \begin{pmatrix} 0,978 & -0,21 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,21 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{Bmatrix} 0,0000 \\ 0,0034 \\ 0,0000 \\ -0,0007 \\ 0,0000 \\ -0,0001 \end{Bmatrix} = \begin{Bmatrix} 174 \\ 37 \\ 326 \\ -174 \\ -37 \\ 254 \end{Bmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\{Fm^A\}_4 = \begin{Bmatrix} 0 \\ 338 \\ 422 \\ 0 \\ 338 \\ -422 \end{Bmatrix} + \begin{pmatrix} 22432000 & 0 & 0 & -22432000 & 0 & 0 \\ 0 & 134827 & 505600 & 0 & -134827 & 505600 \\ 0 & 505600 & 2528000 & 0 & -505600 & 1264000 \\ -22432000 & 0 & 0 & 22432000 & 0 & 0 \\ 0 & -134827 & -505600 & 0 & 134827 & -505600 \\ 0 & 505600 & 1264000 & 0 & -505600 & 2528000 \end{pmatrix} \times \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{Bmatrix} -0,0007 \\ 0,0000 \\ -0,0001 \\ 0 \\ 0 \\ 0 \end{Bmatrix} = \begin{Bmatrix} 0 \\ 178 \\ -254 \\ 0 \\ 497 \\ -945 \end{Bmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$



- **Perhitungan Gaya-Gaya Dalam Akhir Batang (pada sumbu struktur) – Beban Horizontal**

Rumus: $\{F_s^A\}_i = [RT]^T_i \times \{F_m^A\}_i$

dengan: $\{F_s^A\}_i$ = Gaya dalam akhir batang

$[RT]^T_i$ = Matriks rotasi transpose

$\{F_m^A\}_i$ = Gaya dalam batang

$$\{F_s^A\}_1 = \begin{pmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 0 \\ 497 \\ 945 \\ 0 \\ 178 \\ 254 \end{pmatrix} = \begin{pmatrix} -497 \\ 0 \\ 945 \\ -178 \\ 0 \\ 254 \end{pmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}$$

$$\{F_s^A\}_2 = \begin{pmatrix} 0,978 & -0,208 & 0 & 0 & 0 & 0 \\ 0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & -0,208 & 0 \\ 0 & 0 & 0 & 0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 174 \\ -37 \\ -254 \\ -174 \\ 37 \\ -326 \end{pmatrix} = \begin{pmatrix} 178 \\ 0 \\ -254 \\ -178 \\ 0 \\ -326 \end{pmatrix} \begin{matrix} 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

$$\{F_s^A\}_3 = \begin{pmatrix} 0,978 & 0,208 & 0 & 0 & 0 & 0 \\ -0,208 & 0,978 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0,978 & 0,208 & 0 \\ 0 & 0 & 0 & -0,208 & 0,978 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 174 \\ 37 \\ 326 \\ -174 \\ -37 \\ 254 \end{pmatrix} = \begin{pmatrix} 178 \\ 0 \\ 326 \\ -178 \\ 0 \\ 254 \end{pmatrix} \begin{matrix} 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \end{matrix}$$

$$\{F_s^A\}_4 = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} 0 \\ 178 \\ -254 \\ 0 \\ 497 \\ -945 \end{pmatrix} = \begin{pmatrix} 178 \\ 0 \\ -254 \\ 497 \\ 0 \\ -945 \end{pmatrix} \begin{matrix} 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \end{matrix}$$

C.3 Analisis Portal Tidak Bergoyang

➤ Aksi Kolom

- Faktor kekakuan masing-masing elemen:

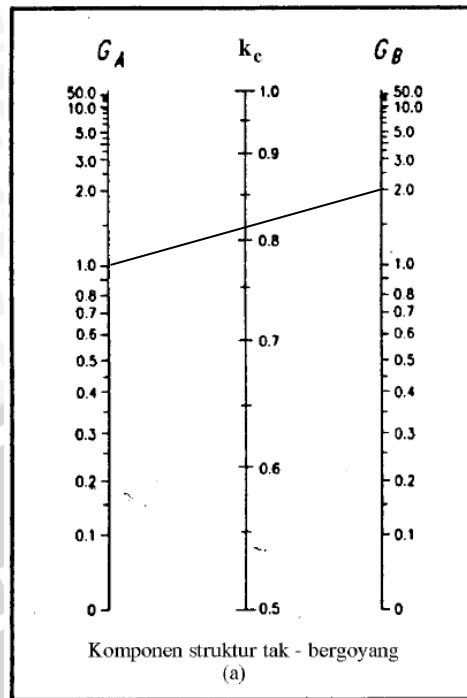
Elemen	$I \text{ (cm}^4\text{)}$	$L \text{ (cm)}$	I/L
12	23700	750	31,6
23	23700	1569	15,10
34	23700	1569	15,10
45	23700	750	31,6

- Faktor G tiap-tiap joint:

Joint	$\sum(I/L)_c / \sum(I/L)_b$	G
1	-	1
2	31,6 / 15,10	2,092
4	31,6 / 15,10	2,092
5	-	1

- Faktor panjang efektif k , masing-masing kolom:

Kolom	G_A	G_B	k
12	1	2,092	1,47
45	2,092	1	1,47



$$k_s = 0,815$$

$$\lambda_c = \frac{1}{\pi} \frac{k_b L}{r_y} \sqrt{\frac{f_y}{E}}$$

$$= \frac{1}{\pi} \frac{1,0 \times 7500}{45,4} \sqrt{\frac{240}{200000}}$$

$$= 1,82157124 \geq 1,2, \text{ maka}$$

$$N_k = \phi A_g \frac{f_y}{1,25 \lambda_c^2}$$

$$= 0,85 \times 8412 \frac{240}{1,25 \times 1,4846^2}$$

$$= 413739,6062 \text{ N}$$

$$\frac{N_u}{N_k} = \frac{44021}{413739,6062} = 0,106397839 < 0,2 \text{ maka memakai persamaan:}$$

$$\frac{N_u}{2\phi N_n} + \frac{M_{ux}}{\phi_b M_{nx}} \leq 1,0$$

➤ Aksi Balok

$$\begin{aligned}\lambda &= \frac{d - 2 \times (r + t_f)}{t_w} \\ &= \frac{400 - 2 \times (16 + 13)}{8} \\ &= 42,75\end{aligned}$$

$$\begin{aligned}N_{ny} &= \frac{N_u}{0,9A_g f_y} \\ &= \frac{44021}{0,9 \times 8412 \times 240} \\ &= 0,024\end{aligned}$$

$N_{ny} \leq 0,125$, maka

$$\begin{aligned}\lambda_p &= \frac{1680}{\sqrt{f_y}} (1 - 2,75 N_{ny}) \\ &= \frac{1680}{\sqrt{240}} (1 - 2,75 \times 0,024) \\ &= 101,2185\end{aligned}$$

$$\begin{aligned}\lambda_r &= \frac{2550}{\sqrt{f_y}} (1 - 0,745 N_{ny}) \\ &= \frac{2550}{\sqrt{240}} (1 - 0,745 \times 0,024) \\ &= 161,631\end{aligned}$$

$(\lambda = 42,75) \leq (\lambda_p = 101,2185)$, merupakan penampang kompak, sehingga

$$\begin{aligned}M_{n1} &= 1,5 f_y S \\ &= 1,5 \times 240 \times 1190000 \\ &= 428400000 \text{ N.mm}\end{aligned}$$

$$\begin{aligned}M_r &= S(f_y - f_r) \\ &= 1190000(240 - 70) \\ &= 202300000 \text{ N.mm}\end{aligned}$$

$$\begin{aligned}M_p &= 1,5 f_y S \\ &= 1,5 \times 240 \times 1190000\end{aligned}$$

= 428400000 N.mm



$$f_L = f_y - f_r$$

$$= 240 - 70$$

$$= 170 \text{ MPa}$$

$$h = d - 2 \times (r + t_f)$$

$$= 400 - 2 \times (16 + 13)$$

$$= 342 \text{ mm}$$

$$I = \sum \frac{1}{3} b t^3$$

$$= \frac{1}{3} (2 \times 200 \times 13^3 + 342 \times 8^3)$$

$$= 351301 \text{ mm}^4$$

$$I_w = \frac{h^2}{4} I_y$$

$$= \frac{342^2}{4} \times 17400000$$

$$= 508793400000 \text{ mm}^6$$

$$X_1 = \frac{\pi}{S} \sqrt{\frac{E G J A}{2}}$$

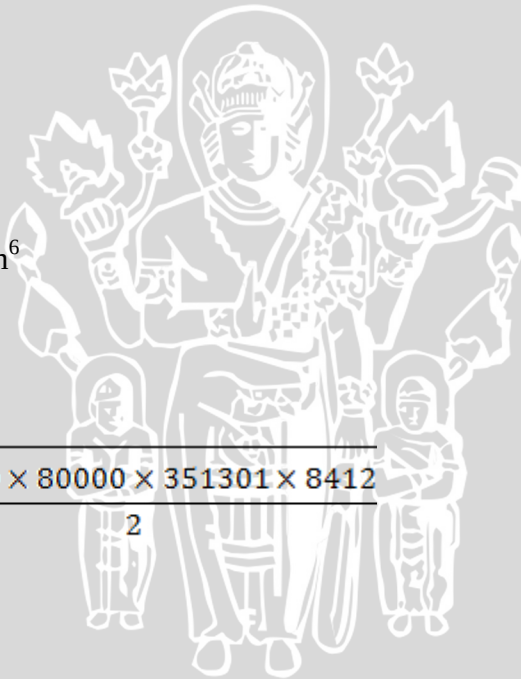
$$= \frac{\pi}{1190000} \sqrt{\frac{200000 \times 80000 \times 351301 \times 8412}{2}}$$

$$= 12836,228 \text{ MPa}$$

$$X_2 = 4 \left(\frac{S_x}{G J} \right)^2 \frac{I_w}{I_y}$$

$$= 4 \left(\frac{1190000}{80000 \times 351301} \right)^2 \frac{508793400000}{17400000}$$

$$= 2,097 \times 10^{-4} (1/\text{MPa})^2$$



$$L_p = 1,76 \sqrt{\frac{I_y \times E}{A \times f_y}}$$

$$= 1,76 \sqrt{\frac{17400000 \times 200000}{8412 \times 240}}$$

$$= 2311 \text{ mm}$$

$$L_r = \frac{X_1}{f_L} \sqrt{\frac{I_y}{A}} \sqrt{1 + \sqrt{1 + X_2 f_L^2}}$$

$$= \frac{12836,228}{170} \sqrt{\frac{17400000}{8412}} \sqrt{1 + \sqrt{1 + 2,097 \times 10^{-4} \times 170^2}}$$

$$= 6567 \text{ mm}$$

$(L_p = 2311) < (L_r = 6567) < (L = 7500)$, merupakan bentang panjang, sehingga

PERHITUNGAN M_A , M_B , M_C

x →			0	3,9232	7,8465	11,77	15,693		
M	-13203		-13203	-13203	-13203	-13203	-13203		
q	-87		0	-641,5	-2566	-5773	-10264		
P	-790	x cos12 = -773	0	-3031	-6062	-9093	-12124		
V2	4402	x cos12 = 4306	0	16893	33786	50679	67572		
H2	-3259	x sin12 = -678	0	-2658	-5316	-7974	-10633		
1,30	-196	x cos12 = -192		-503	-1254	-2006	-2757		
2,60				-254	-1005	-1757	-2508		
3,90				-4	-756	-1508	-2259		
5,20					-507	-1259	-2010		
6,50					-258	-1010	-1761		
7,80					-9	-761	-1512		
9,10						-511	-1263		
10,40						-262	-1014		
11,70						-13	-765		
13,00							-516		
14,30							-267		
Jumlah			-13203	-3401	2849	5549	4715		
				M _A	M _B	M _C			

$$C_b = \frac{12,5M_u}{2,5M_u + 3M_A + 4M_B + 3M_C}$$

$$= \frac{12,5 \times 13203}{2,5 \times 13203 + 3 \times 3401 + 4 \times 2849 + 3 \times 5549}$$

$$= 2,316$$



$$M_{n2} = C_b \frac{\pi}{L} \sqrt{EI_y GJ + \left(\frac{\pi E}{L}\right)^2 I_y I_w}$$

$$= 2,316 \frac{\pi}{7500} \sqrt{2 \times 10^5 \times 1,74 \times 10^7 \times 8 \times 10^4 + 351301 + \left(\frac{\pi \times 2 \times 10^5}{7500}\right)^2 \times 1,74 \times 10^7 \times 508793400000}$$

$$M_{n2} = 388006196 < M_{n1} = 428400000, \text{ maka}$$

$$M_{nx} = M_{n2} = 388006196 \text{ N.mm}$$

➤ **Perbesaran Momen Struktur Tak Bergoyang**

$$C_m = 0,6 - 0,4 \frac{M_1}{M_2}$$

$$= 0,6 - 0,4 \frac{11238}{13203}$$

$$= 0,260$$

$$N_{crb} = \frac{\pi^2 EA_g}{(k_b L/r_x)^2}$$

$$= \frac{\pi^2 \times 200000 \times 8412}{(1,0 \cdot 7500/168)^2}$$

$$= 8331535 \text{ N}$$

$$\delta_b = \frac{C_m}{1 - \frac{N_u}{N_{crb}}}$$

$$= \frac{0,260}{1 - \frac{44021}{8331535}}$$

$$= 0,261 < 1 \rightarrow \text{diambil } 1$$

➤ **Periksa Persamaan Balok Kolom**

$$M_{ux} = \delta_b M_{ntu}$$

$$= 1 \times 132031512$$

$$= 132031512 \text{ N.mm}$$

$$\frac{N_u}{2\phi N_n} + \frac{M_{ux}}{\phi_b M_{nx}} \leq 1,0$$



$$\frac{0,1064}{2} + \frac{132031512}{0,9 \times 388006196} = 0,4313 \leq 1,0 \rightarrow \text{AMAN \& SANGAT BOROS}$$

C.4 Analisis Portal Bergoyang

➤ Aksi Kolom (Gravitasi)

$$\frac{N_u}{N_k} = \frac{61896}{413739,6062} = 0,1496 < 0,2 \text{ maka memakai persamaan:}$$

$$\frac{N_u}{2\phi N_n} + \frac{M_{ux}}{\phi_b M_{nx}} \leq 1,0$$

➤ Aksi Balok (Gravitasi)

$$\begin{aligned} N_{ny} &= \frac{N_u}{0,9 A_g f_y} \\ &= \frac{61896}{0,9 \times 8412 \times 240} \\ &= 0,034 \end{aligned}$$

$N_{ny} \leq 0,125$, maka

$$\begin{aligned} \lambda_p &= \frac{1680}{\sqrt{f_y}} (1 - 2,75 N_{ny}) \\ &= \frac{1680}{\sqrt{240}} (1 - 2,75 \times 0,034) \\ &= 98,284 \\ \lambda_r &= \frac{2550}{\sqrt{f_y}} (1 - 0,745 N_{ny}) \\ &= \frac{2550}{\sqrt{240}} (1 - 0,745 \times 0,034) \\ &= 160,424 \end{aligned}$$

$(\lambda = 42,75) \leq (\lambda_p = 98,284)$, merupakan penampang kompak, sehingga

$$M_{n1} = 428400000 \text{ N.mm}$$

$$L_p = 2311 \text{ mm}$$

$$L_r = 6567 \text{ mm}$$

$(L_p = 2311) < (L_r = 6567) < (L = 7500)$, merupakan bentang panjang, sehingga

PERHITUNGAN M_A , M_B , M_C

x →		0	3,9232	7,8465	11,77	15,693
M	-19281	-19281	-19281	-19281	-19281	-19281
q	-87	0	-641	-2566	-5773	-10264
P	-933 x cos12 = -912	0	-3580	-7160	-10740	-14319
V2	6190 x cos12 = 6054	0	23752	47505	71257	95010
H2	-4758 x sin12 = -989	0	-3881	-7762	-11643	-15524
1,30	-339 x cos12 = -331		-869	-2170	-3470	-4771
2,60			-439	-1739	-3039	-4340
3,90			-8	-1308	-2608	-3909
5,20				-877	-2178	-3478
6,50				-446	-1747	-3047
7,80				-15	-1316	-2616
9,10					-885	-2185
10,40					-454	-1754
11,70					-23	-1323
13,00						-893
14,30						-462
Jumlah		-19281	-4947	4180	8100	6843
			M _A	M _B	M _C	

$$C_b = \frac{12,5M_u}{2,5M_u + 3M_A + 4M_B + 3M_C}$$

$$= \frac{12,5 \times 19281}{2,5 \times 19281 + 3 \times 4947 + 4 \times 4180 + 3 \times 8100}$$

$$= 2,316$$

$$M_{n2} = C_b \frac{\pi}{L} \sqrt{EI_y GJ + \left(\frac{\pi E}{L}\right)^2 I_y I_w}$$

$$= 2,316 \frac{\pi}{7500} \sqrt{2 \times 10^5 \times 1,74 \times 10^7 \times 8 \times 10^4 \times 351301 + \left(\frac{\pi \times 2 \times 10^5}{7500}\right)^2 \times 1,74 \times 10^7 \times 508793400000}$$

$$M_{n2} = 387982186 < M_{n1} = 428400000, \text{ maka}$$

$$M_{nx} = M_{n2} = 387982186 \text{ N.mm}$$

➤ **Perbesaran Momen Struktur Tak Bergoyang**

$$C_m = 0,6 - 0,4 \frac{M_1}{M_2}$$

$$= 0,6 - 0,4 \frac{16404}{19281}$$

$$= 0,260$$

$$N_{crb} = \frac{\pi^2 E A_g}{(k_b L / r_x)^2}$$

$$N_{crb} = 8331535 \text{ N}$$

$$\delta_b = \frac{C_m}{1 - \frac{N_u}{N_{crb}}}$$

$$= \frac{0,260}{1 - \frac{61896}{8331535}}$$

$$= 0,262 < 1 \rightarrow \text{diambil } 1$$

➤ **Periksa Persamaan Balok Kolom (Gravitasi)**

$$M_{ux} = \delta_b M_{ntu}$$

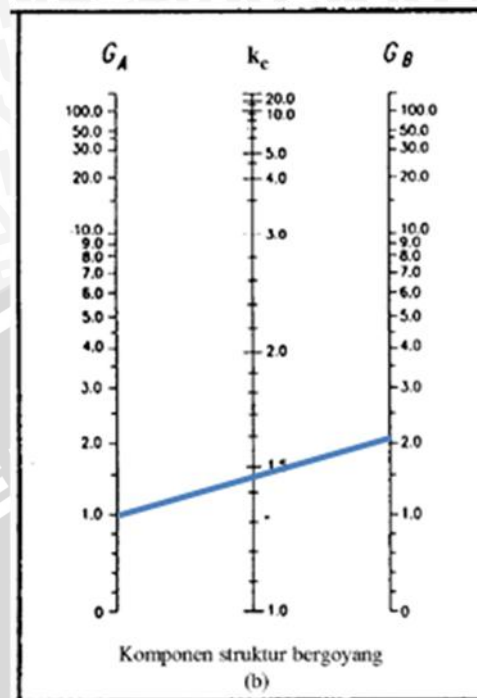
$$= 1 \times 192814828$$

$$= 192814828 \text{ N.mm}$$

$$\frac{N_u}{2\phi N_n} + \frac{M_{ux}}{\phi_b M_{nx}} \leq 1,0$$

$$\frac{0,1496}{2} + \frac{192814828}{0,9 \times 387982186} = 0,627 \leq 1,0 \rightarrow \text{AMAN \& SANGAT BOROS}$$

➤ Aksi Kolom (Gravitasi + Angin)



$$k_s = 1,47$$

$$\frac{N_u}{N_k} = \frac{61900}{413739,6062} = 0,1496 < 0,2 \text{ maka memakai persamaan:}$$

$$\frac{N_u}{2\phi N_n} + \frac{M_{ux}}{\phi_b M_{nx}} \leq 1,0$$

➤ Aksi Balok (Gravitasi + Angin)

$$\begin{aligned} N_{ny} &= \frac{N_u}{0,9A_g f_y} \\ &= \frac{61900}{0,9 \times 8412 \times 240} \\ &= 0,034 \end{aligned}$$

$$N_{ny} \leq 0,125, \text{ maka}$$

$$\begin{aligned} \lambda_p &= \frac{1680}{\sqrt{f_y}} (1 - 2,75N_{ny}) \\ &= \frac{1680}{\sqrt{240}} (1 - 2,75 \times 0,034) \\ &= 98,284 \end{aligned}$$



$$\begin{aligned}\lambda_r &= \frac{2550}{\sqrt{f_y}} (1 - 0,745 N_{ny}) \\ &= \frac{2550}{\sqrt{240}} (1 - 0,745 \times 0,034) \\ &= 160,424\end{aligned}$$

$(\lambda = 42,75) \leq (\lambda_p = 98,284)$, merupakan penampang kompak, sehingga

$$M_{n1} = 428400000 \text{ N.mm}$$

$$L_p = 2311 \text{ mm}$$

$$L_r = 6567 \text{ mm}$$

$(L_p = 2311) < (L_r = 6567) < (L = 7500)$, merupakan bentang panjang, sehingga

PERHITUNGAN M_A , M_B , M_C

x →		0	3,9232	7,8465	11,77	15,693
M	-19028	-19028	-19028	-19028	-19028	-19028
q	-87	0	-641	-2566	-5773	-10264
P	-933	x cos12 = -912	0	-3580	-7160	-10740
V2	6190	x cos12 = 6054	0	23752	47505	71257
H2	-4936	x sin12 = -1026	0	-4026	-8052	-12078
1,30	-339	x cos12 = -331		-869	-2170	-3470
2,60				-439	-1739	-3039
3,90				-8	-1308	-2608
5,20					-877	-2178
6,50					-446	-1747
7,80					-15	-1316
9,10						-885
10,40						-454
11,70						-23
13,00						-892,6
14,30						-461,7
Jumlah		-19028	-4839	4144	7918	6517
			M_A	M_B	M_C	

$$\begin{aligned}C_b &= \frac{12,5M_u}{2,5M_u + 3M_A + 4M_B + 3M_C} \\ &= \frac{12,5 \times 19028}{2,5 \times 19028 + 3 \times 4839 + 4 \times 4144 + 3 \times 7918} \\ &= 2,322\end{aligned}$$

$$M_{n2} = C_b \frac{\pi}{L} \sqrt{EI_y GJ + \left(\frac{\pi E}{L}\right)^2 I_y I_w}$$

$$= 2,322 \frac{\pi}{7500} \sqrt{\frac{2 \times 10^5 \times 1,74 \times 10^7 \times 8 \times 10^4 \times 351301}{7500} + \left(\frac{\pi \times 2 \times 10^5}{7500}\right)^2 \times 1,74 \times 10^7 \times 508793400000}$$

$$M_{n2} = 389045004 < M_{n1} = 428400000, \text{ maka}$$

$$M_{nx} = M_{n2} = 389045004 \text{ N.mm}$$

➤ **Perbesaran Momen Struktur Tak Bergoyang**

$$C_m = 0,6 - 0,4 \frac{M_1}{M_2}$$

$$= 0,6 - 0,4 \frac{15459}{19028}$$

$$= 0,275$$

$$N_{crb} = \frac{\pi^2 EA_g}{(k_b L/r_x)^2}$$

$$N_{crb} = 8331535 \text{ N}$$

$$\delta_b = \frac{C_m}{1 - \frac{N_u}{N_{crb}}}$$

$$= \frac{0,275}{1 - \frac{61900}{8331535}}$$

$$= 0,277 < 1 \rightarrow \text{diambil } 1$$

➤ **Perbesaran Momen Struktur Bergoyang**

$$N_{crs} = \frac{\pi^2 EA_g}{(k_s L/r_x)^2}$$

$$= \frac{\pi^2 \times 200000 \times 8412}{(1,47 \frac{7500}{168})^2}$$

$$= 3855586 \text{ N}$$

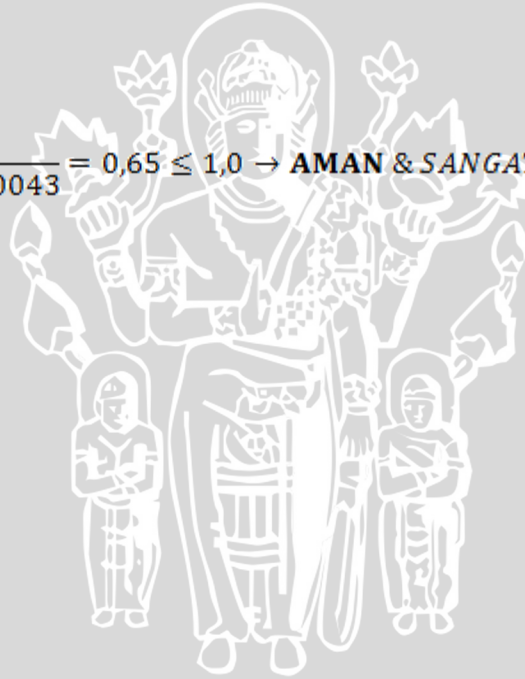


$$\begin{aligned}\delta_s &= \frac{1}{1 - \frac{N_u}{N_{crs}}} \\ &= \frac{1}{1 - \frac{61900}{3855586}} \\ &= 1,016\end{aligned}$$

➤ **Periksa Persamaan Balok Kolom (Gravitasi + Angin)**

$$\begin{aligned}M_{ux} &= \delta_b M_{ntu} + \delta_s M_{itu} \\ &= 1 \times 192814828 + 1,016 \times 9451360 \\ &= 202420402 \text{ N.mm}\end{aligned}$$

$$\begin{aligned}\frac{N_u}{2\phi N_n} + \frac{M_{ux}}{\phi_b M_{nx}} &\leq 1,0 \\ \frac{0,1496}{2} + \frac{202420402}{0,9 \times 3890450043} &= 0,65 \leq 1,0 \rightarrow \text{AMAN \& SANGAT BOROS}\end{aligned}$$



Lampiran 7. *Form (Code) Program*

```

Private Sub Command1_Click()
    ANny = Val(TextNu) / (0.9 * Val(TextAg) * Val(Tfy))
    If ANny <= 0.125 Then
        LamdaP = 1680 * (1 - 2.75 * ANny) / Sqr(Tfy)
    ElseIf ANny > 0.125 Then
        LamdaP2 = 500 * (2.33 - ANny) / Sqr(Tfy)
        If LamdaP2 >= 665 / Sqr(Tfy) Then
            LamdaP = 500 * (2.33 - ANny) / Sqr(Tfy)
        ElseIf LamdaP2 < 665 / Sqr(Tfy) Then
            LamdaP = 665 / Sqr(Tfy)
        End If
    End If
    AMr = TSx * (Tfy - Tfr)
    Amp = 1.5 * Tfy * TSx
    Lamda = (Textd - (2 * (Val(Textr) + Val(Ttf)))) / Ttw
    LamdaR = 2550 * (1 - (0.745 * ANny)) / Sqr(Tfy)
    If LamdaR <= Lamda Then
        Mn1 = AMr * ((LamdaR / Lamda) ^ 2)
        LPenampang.Caption = "PENAMPANG LANGSING"
    ElseIf Lamda <= LamdaP Then
        Mn1 = 1.5 * Tfy * TSx
        LPenampang.Caption = "PENAMPANG KOMPAK"
    Else
        Mn1 = Amp - ((Amp - AMr) * (Lamda - LamdaP) / (LamdaR - LamdaP))
        LPenampang.Caption = "PENAMPANG TIDAK KOMPAK"
    End If
    Afl = Tfy - Tfr
    h = Textd - (2 * (Val(Textr) + Val(Ttf)))
    J = (2 * Tbf * (Ttf ^ 3) + Val(h) * (Ttw ^ 3)) / 3
    Iw = (h ^ 2) * TIy / 4

```


$X1 = 3.141592654 * ((\text{Val}(\text{TextE}) * \text{Val}(\text{TextG}) * J * \text{Val}(\text{TextAg}) / 2) ^ 0.5) / \text{Val}(\text{TSx})$

$X2 = 4 * ((\text{Val}(\text{TSx}) / (\text{TextG} * J)) ^ 2) * Iw / \text{Val}(\text{TIy})$

$Cb = 12.5 * \text{TMu} / (2.5 * \text{TMu} + 3 * \text{TMa} + 4 * \text{TMb} + 3 * \text{TMc})$

$Lp = 1.76 * ((\text{TIy} * \text{TextE} / (\text{TextAg} * \text{Tfy})) ^ 0.5)$

$Lr = X1 * ((\text{TIy} / \text{TextAg}) ^ 0.5) * ((1 + ((1 + ((\text{Afl} ^ 2) * X2)) ^ 0.5)) ^ 0.5) / \text{Afl}$

If $Lr \leq \text{Val}(\text{TextL})$ Then

$\text{Mcr} = Cb * 3.141592654 * (((\text{Val}(\text{TextE}) * \text{Val}(\text{TIy}) * \text{Val}(\text{TextG}) * J) + ((3.141592654 * \text{Val}(\text{TextE}) / \text{Val}(\text{TextL})) ^ 2) * \text{Val}(\text{TIy}) * Iw)) ^ 0.5) / \text{Val}(\text{TextL})$

If $\text{Mcr} \leq \text{AMp}$ Then

$\text{Mn2} = \text{Mcr}$

$\text{LLateral.Caption} = \text{"PENAMPANG BENTANG PANJANG"}$

ElseIf $\text{Mcr} > \text{AMp}$ Then

$\text{Mn2} = \text{AMp}$

$\text{LLateral.Caption} = \text{"PENAMPANG BENTANG PANJANG"}$

End If

ElseIf $\text{Val}(\text{TextL}) \leq Lp$ Then

$\text{Mn2} = \text{AMp}$

$\text{LLateral.Caption} = \text{"PENAMPANG BENTANG PENDEK"}$

Else

$\text{Mn2} = Cb * (\text{AMr} + ((\text{AMp} - \text{AMr}) * (Lr - \text{Val}(\text{TextL})) / (Lr - Lp)))$

$\text{LLateral.Caption} = \text{"PENAMPANG BENTANG MENENGAH"}$

End If

If $\text{Mn1} > \text{Mn2}$ Then

$\text{Mnx} = \text{Mn2}$

Else

$\text{Mnx} = \text{Mn1}$

End If

$\text{Ncrb} = (3.141592654 ^ 2) * \text{TextE} * \text{Val}(\text{TextAg}) / ((\text{Tkb} * \text{TextL} / \text{Textrx}) ^ 2)$

$\text{Sbb} = \text{TCm} / (1 - (\text{Val}(\text{TextNu}) / \text{Ncrb}))$

If $\text{Sbb} \geq 1$ Then

$\text{Sb} = \text{Sbb}$

Else

$\text{Sb} = 1$

```

End If
Ncrs = (3.141592654 ^ 2) * TextE * Val(TextAg) / ((Tks * TextL / Textrx) ^ 2)
Sss = TCm / (1 - (Val(TextNu) / Ncrs))
If Sss >= 1 Then
    Ss = Sss
Else
    Ss = 1
End If
Mux = (Sb * TMntu) + (Ss * TMltu)
ALk = Tks * TextL
Lamdac = ALk * ((Val(Tfy) / Val(TextE)) ^ 0.5) / (3.141592654 * Val(Textry))
If Lamdac <= 0.25 Then
    Nkk = 0.85 * Val(TextAg) * Val(Tfy)
ElseIf Lamdac >= 1.2 Then
    Nkk = 0.85 * Val(TextAg) * Val(Tfy) / (1.25 * (Lamdac ^ 2))
Else
    Nkk = 0.85 * Val(TextAg) * Val(Tfy) * (1.6 - (0.67 * Lamdac)) / 1.43
End If
bantu2 = TextNu / Nkk
AMmy = Mux / (0.9 * Mnx)
If bantu2 >= 0.2 Then
    bantu3 = ANny + (8 * AMmy / 9)
    If bantu3 <= 1 Then
        bantu3 = ANny + (8 * AMmy / 9)
        If bantu3 <= 0.7 Then
            Labelc = "Profil yang Anda pakai AMAN namun SANGAT BOROS"
            LabelM = bantu3
        ElseIf bantu3 >= 0.9 Then
            Labelc = "Profil yang Anda pakai AMAN dan EFISIEN"
            LabelM = bantu3
        Else
            Labelc = "Profil yang Anda pakai AMAN namun CUKUP BOROS"
            LabelM = bantu3
        End If
    End If

```

```

Else
Labelc = "Profil yang Anda pakai TIDAK AMAN"
LabelM = bantu3
End If
ElseIf bantu2 < 0.2 Then
bantu4 = (0.5 * ANny) + AMmy
If bantu4 <= 1 Then
bantu4 = (0.5 * ANny) + AMmy
If bantu4 <= 0.7 Then
Labelc = "Profil yang Anda pakai AMAN namun SANGAT BOROS"
LabelM = bantu4
ElseIf bantu4 >= 0.9 Then
Labelc = "Profil yang Anda pakai AMAN dan EFISIEN"
LabelM = bantu4
Else
Labelc = "Profil yang Anda pakai AMAN namun CUKUP BOROS"
LabelM = bantu4
End If
Else
Labelc = "Profil yang Anda pakai TIDAK AMAN"
LabelM = bantu4
End If
End If
End Sub

```

```

Private Sub Command2_Click()
ANny = Val(TextNu) / (0.9 * Val(TextAg) * Val(Tfy))
If ANny <= 0.125 Then
LamdaP = 1680 * (1 - 2.75 * ANny) / Sqr(Tfy)
ElseIf ANny > 0.125 Then
LamdaP2 = 500 * (2.33 - ANny) / Sqr(Tfy)
If LamdaP2 >= 665 / Sqr(Tfy) Then
LamdaP = 500 * (2.33 - ANny) / Sqr(Tfy)
ElseIf LamdaP2 < 665 / Sqr(Tfy) Then

```



```

    LamdaP = 665 / Sqr(Tfy)
End If
End If
AMr = TSx * (Tfy - Tfr)
AMp = 1.5 * Tfy * TSx
Lamda = (Textd - (2 * (Val(Textr) + Val(Ttf)))) / Ttw
LamdaR = 2550 * (1 - (0.745 * ANny)) / Sqr(Tfy)
If LamdaR <= Lamda Then
    Mn1 = AMr * ((LamdaR / Lamda) ^ 2)
    LPenampang.Caption = "PENAMPANG LANGSING"
ElseIf Lamda <= LamdaP Then
    Mn1 = 1.5 * Tfy * TSx
    LPenampang.Caption = "PENAMPANG KOMPAK"
Else
    Mn1 = AMp - ((AMp - AMr) * (Lamda - LamdaP) / (LamdaR - LamdaP))
    LPenampang.Caption = "PENAMPANG TIDAK KOMPAK"
End If
Afl = Tfy - Tfr
h = Textd - (2 * (Val(Textr) + Val(Ttf)))
J = (2 * Tbf * (Ttf ^ 3) + Val(h) * (Ttw ^ 3)) / 3
Iw = (h ^ 2) * TIy / 4
X1 = 3.141592654 * ((Val(TextE) * Val(TextG) * J * Val(TextAg) / 2) ^ 0.5) /
Val(TSx)
X2 = 4 * ((Val(TSx) / (TextG * J)) ^ 2) * Iw / Val(TIy)
Cb = 12.5 * TMu / (2.5 * TMu + 3 * TMa + 4 * TMb + 3 * TMc)
Lp = 1.76 * ((TIy * TextE / (TextAg * Tfy)) ^ 0.5)
Lr = X1 * ((TIy / TextAg) ^ 0.5) * ((1 + ((1 + ((Afl ^ 2) * X2)) ^ 0.5)) ^ 0.5) / Afl
If Lr <= Val(TextL) Then
    Mcr = Cb * 3.141592654 * (((Val(TextE) * Val(TIy) * Val(TextG) * J) +
    (((3.141592654 * Val(TextE) / Val(TextL)) ^ 2) * Val(TIy) * Iw)) ^ 0.5) / Val(TextL)
    If Mcr <= AMp Then
        Mn2 = Mcr
        LLLateral.Caption = "PENAMPANG BENTANG PANJANG"
    ElseIf Mcr > AMp Then

```

```

Mn2 = AMp
LLateral.Caption = "PENAMPANG BENTANG PANJANG"
End If
ElseIf Val(TextL) <= Lp Then
Mn2 = AMp
LLateral.Caption = "PENAMPANG BENTANG PENDEK"
Else
Mn2 = Cb * (AMr + ((AMp - AMr) * (Lr - Val(TextL)) / (Lr - Lp)))
LLateral.Caption = "PENAMPANG BENTANG MENENGAH"
End If
If Mn1 > Mn2 Then
Mnx = Mn2
Else
Mnx = Mn1
End If
LabelM = Mnx
Ncrb = (3.141592654 ^ 2) * TextE * Val(TextAg) / ((Tkb * TextL / Textrx) ^ 2)
Sbb = TCm / (1 - (Val(TextNu) / Ncrb))
If Sbb >= 1 Then
Sb = Sbb
Else
Sb = 1
End If
Mux = Sb * TMntu
ALk = Tkb * TextL
Lamdac = ALk * ((Val(Tfy) / Val(TextE)) ^ 0.5) / (3.141592654 * Val(Trxy))
If Lamdac <= 0.25 Then
Nkk = 0.85 * Val(TextAg) * Val(Tfy)
ElseIf Lamdac >= 1.2 Then
Nkk = 0.85 * Val(TextAg) * Val(Tfy) / (1.25 * (Lamdac ^ 2))
Else
Nkk = 0.85 * Val(TextAg) * Val(Tfy) * (1.6 - (0.67 * Lamdac)) / 1.43
End If
bantu2 = TextNu / Nkk

```

```
AMmy = Mux / (0.9 * Mnx)
If bantu2 >= 0.2 Then
    bantu3 = ANny + (8 * AMmy / 9)
    If bantu3 <= 1 Then
        bantu3 = ANny + (8 * AMmy / 9)
        If bantu3 <= 0.7 Then
            Labelc = "Profil yang Anda pakai AMAN namun SANGAT BOROS"
            LabelM = bantu3
        ElseIf bantu3 >= 0.9 Then
            Labelc = "Profil yang Anda pakai AMAN dan EFISIEN"
            LabelM = bantu3
        Else
            Labelc = "Profil yang Anda pakai AMAN namun CUKUP BOROS"
            LabelM = bantu3
        End If
    Else
        Labelc = "Profil yang Anda pakai TIDAK AMAN"
        LabelM = bantu3
    End If
ElseIf bantu2 < 0.2 Then
    bantu4 = (0.5 * ANny) + AMmy
    If bantu4 <= 1 Then
        bantu4 = (0.5 * ANny) + AMmy
        If bantu4 <= 0.7 Then
            Labelc = "Profil yang Anda pakai AMAN namun SANGAT BOROS"
            LabelM = bantu4
        ElseIf bantu4 >= 0.9 Then
            Labelc = "Profil yang Anda pakai AMAN dan EFISIEN"
            LabelM = bantu4
        Else
            Labelc = "Profil yang Anda pakai AMAN namun CUKUP BOROS"
            LabelM = bantu4
        End If
    Else
```


Labelc = "Profil yang Anda pakai TIDAK AMAN"

LabelM = bantu4

End If

End If

End Sub

Private Sub Command3_Click()

TextE.Text = ""

Tfr.Text = ""

Tfy.Text = ""

TextG.Text = ""

TextL.Text = ""

Textd.Text = ""

Tbf.Text = ""

TextAg.Text = ""

Tweight.Text = ""

Ttf.Text = ""

Ttw.Text = ""

Tly.Text = ""

Textr.Text = ""

TSx.Text = ""

Textrx.Text = ""

Textry.Text = ""

TNu.Text = ""

TMu.Text = ""

TMa.Text = ""

TMb.Text = ""

TMc.Text = ""

Tkb.Text = ""

Tks.Text = ""

TCm.Text = ""

TMntu.Text = ""

TMltu.Text = ""



LLateral.Caption = ""

LPenampang.Caption = ""

Labelk.Caption = ""

LabelM.Caption = ""

Labelc.Caption = ""

End Sub

Private Sub Command4_Click()

End

End Sub

Private Sub Tbf_Change()

Labelk = "Lebar Profil"

End Sub

Private Sub TCm_Change()

Labelk = "Koefisien lentur kolom (struktur tak bergoyang tanpa beban transversal = 0,6
- 0,4Bm; Ujung sederhana = 1; Ujung kaku = 0,85"

End Sub

Private Sub TextAg_Change()

Labelk = "Luas penampang"

End Sub

Private Sub Textd_Change()

Labelk = "Tinggi profil"

End Sub

Private Sub TextE_Change()

Labelk = "Modulus elastisitas baja "

End Sub

Private Sub TextG_Change()

Labelk = "Moudulus geser baja "

End Sub

Private Sub TextL_Change()

Labelk = "Panjang komponen struktur"

End Sub

Private Sub TextR_Change()

Labelk = "Jari-jari peralihan penampang"

End Sub

Private Sub Textrx_Change()

Labelk = "Jari-jari girasi komponen struktur terhadap sumbu-x"

End Sub

Private Sub Textry_Change()

Labelk = "Jari-jari girasi terhadap sumbu-y"

End Sub

Private Sub Tfr_Change()

Labelk = "Tegangan tekan sisa pada pelat sayap, diambil sebesar 70 MPa untuk penampang dirol dan 115 MPa untuk penampang dilas"

End Sub

Private Sub Tfy_Change()

Labelk = "Tegangan leleh"

End Sub

Private Sub TIy_Change()

Labelk = "Momen inersia terhadap sumbu-y"

End Sub

Private Sub Tkb_Change()

Labelk = "Faktor panjang tekuk untuk struktur tidak bergoyang"

End Sub

Private Sub Tks_Change()

Labelk = "Faktor panjang tekuk untuk struktur bergoyang"

End Sub

Private Sub TMa_Change()

Labelk = "Momen lentur pada 1/4 bentang"

End Sub

Private Sub TMb_Change()

Labelk = "Momen lentur pada tengah bentang"

End Sub

Private Sub TMc_Change()

Labelk = "Momen lentur pada 3/4 bentang"

End Sub

Private Sub TMltu_Change()

Labelk = "Momen lentur terfaktor yang diakibatkan oleh beban-beban yang dapat menimbulkan goyangan"

End Sub

Private Sub TMntu_Change()

Labelk = "Momen lentur terfaktor yang diakibatkan oleh beban-beban yang tidak menimbulkan goyangan"

End Sub

Private Sub TMu_Change()

Labelk = "Momen lentur terfaktor maksimal pada struktur"

End Sub

Private Sub TNu_Change()

Labelk = "Gaya aksial terfaktor tekan yang terbesar pada komponen struktur"

End Sub

Private Sub TSx_Change()

Labelk = "Modulus penampang elastis"

End Sub

Private Sub Ttf_Change()

Labelk = "Tebal pelat sayap"

End Sub

Private Sub Ttw_Change()

Labelk = "Tebal pelat badan"

End Sub

Private Sub Tweight_Change()

Labelk = "Berat penampang"

End Sub

